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Threshold effects in purchasing power parity for African Countries

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This study applies non-linear threshold unit-root test to assess the non-stationary properties of the real exchange rate for twenty African countries. We found that non-linear threshold unit-root test has higher power than linear method. As suggested by Caner and Hansen (2001), the true data generating process of exchange rate is a stationary non-linear process. We examine the validity of PPP from the non-linear point of view and provide robust evidence clearly indicating that purchasing power parity (PPP) holds true for six countries, namely; Egypt, Ethiopia, Gambia, Malawi, Seychelles and South Africa. Our findings point out their exchange rate adjustment is mean reversion towards PPP equilibrium values in a non-linear way.

Key words: Non-linear threshold unit-root test, purchasing power parity.

INTRODUCTION

The analysis of long-run purchasing power parity (PPP) has probably been one of the most controversial topics of the last decades within international economics. The results from validity of PPP have important implications to decision or policy makers of central banks, multinational firms and exchange rate market participants. The exchange rate policy is often regarded as the centerpiece of economic reform programmers, and the external competitiveness of any particular country is frequently gauged by the movement of its real exchange rate. The results from studies in this regard are critical for both empirical researchers and policymakers. PPP also provides an important basis for financial stabilization and structural adjustment policies and plays a role in the choice between money, inflation or exchange rate targeting in the formulation of monetary policy. In particular, the long-run PPP requires that real exchange rates must be stationary, which implies there is a long-run relationship between nominal exchange rate, domestic and foreign prices. As such, PPP cannot be used to determine the equilibrium exchange rate and invalid PPP also disqualifies the monetary approach to exchange rate

determination, which requires PPP to hold true. According to Holmes (2001), the PPP is important to policy makers for two reasons.

First of all, it can be used to predict exchange rate to determine whether a currency is over or undervalued. Whether a currency is over or undervalued is particularly important for less-developed countries and also for those experiencing large difference between domestic and foreign inflation rates.

Secondly, the notion of PPP is used as the foundation on which many theories of exchange rate determination are built. Consequently, the validity is important to those policy makers in developing countries who base their adjustment on the PPP.

While empirical evidence shows that stationarityy of the real exchange rate (RER) is abundant in developing countries (Bahmani-Oskooee, 1995; Breuer et al., 2001). Few studies have been conducted using date from small developing countries and, in particular, from Africa. Besides, robust researches on PPP are very important for African countries to the extent that, since the early 1990s, these have implemented numerous exchange rate policies' modifications based on the assumption of PPP validity (Kargbo, 2003).

Recently, several studies have examined whether or not there is empirical support for long-run PPP in African countries (Odekokun, 2000; Holmes, 2000; Nagayasu,

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2002; Kargbo, 2006; Hassanain, 2004; Akinboade and Makina, 2006; Bahmanee-Oskooee and Gelan, 2006). But, once again, a strong consensus could not be reached even if more results converge towards PPP validity.

For the past two decades, African countries have been implementing structural and macro-economic adjustment programmes designed to improve the external competitiveness and economic growth of these economies (Kargbo, 2004). In particular, exchange rate policy reforms were the focal point of the adjustment programmes.

Empirical research on PPP has therefore focused on the credibility of the unit root finding and on why deviations from PPP exist.

Despite a decade of multiple applications of the unit root tests in analyzing PPP, we are still unable to draw homogenous conclusions.

For previous studies, one possible explanation for the inconsistencies in the existing empirical evidence on the PPP hypothesis is that the prior studies implicitly assume that exchange rate behavior is inherently linear in nature. It is well know that if RER follows nonlinear stationary process then tests based on linear models such as the widely used augmented Dickey-Fuller (ADF) unit root models will be mis-specified (Chortareas et al., 2002).

However, Sarno (2000) and Taylor and Peel (2000) also demonstrated that the adoption of linear stationarity tests is inappropriate for the detection of mean reversion if the true process of the data generation of the exchange rate is in fact a stationary non-linear process. The presence of nonlinear mean-reverting adjustment for real exchange rates has been advanced by recent theoretical developments that emphasize the role of transaction costs. Taylor et al. (2001), Taylor and Peel (2000), Taylor and Taylor (2004), Juvenal and Taylor (2008) and Lothian and Taylor (2008) have argued that different speeds of adjustment at the disaggregated goods level average up to smooth nonlinearity at the aggregate level.

An alternative view is that non-linearity at the aggregate level is caused by other influences, such as the effects of official foreign exchange intervention (Taylor, 2004; Menkhof and Taylor, 2007; Reitz and Taylor, 2008) or heterogeneous agents (Kilian and Taylor, 2003). Additionally, the existence of structure changes in the RER might imply broken deterministic time trends and the result is a nonlinear pattern (Bierens, 1997).

The central aim of this study contributes significantly to this field of research because, first of all, we examine evidence for PPP for African countries, using the threshold autoregressive model (TAR) and the test statistics suggested by Caner and Hansen (2001). The main advantage of this procedure is that it allows one to simultaneously test for non-linearities and non stationarity.

Secondly, to the best of our knowledge, this study is the first of its kind to utilize the threshold unit root test for long-run PPP in African countries.

THRESHOLD UNIT-ROOT TEST METHODOLOGY

Here, we test the threshold effect on the unit root process of the real exchange rate series r_t using the threshold unit root model developed by Caner and Hansen (2001), who considered a two regime TAR(k) model:

$$\Delta r_{t} = \theta_{1}' x_{t-1} I_{Z_{i} \leq \lambda} + \theta_{2}' x_{t-1} I_{Z_{i} > \lambda} + e_{t}, \quad t = 1, \dots, T$$
(1)

Where, $x_{t-1} = (r_{t-1}, v_t', \Delta r_{t-1}, ..., \Delta r_{t-k})'$, I_{\bullet} is the indicator function, e_t is an i.i.d. disturbance, $Z_{t-1} = r_{t-1} - r_{t-m}$

for some $m \geq 1$ is the threshold variable, v_t is a vector of exogenous variables including an intercept and possibly a linear time trend, λ is a threshold parameter and $k \geq 1$ is the autoregressive unit root. The components of θ_1 and θ_2 can be partitioned as follows:

$$\theta_1 = \begin{pmatrix} \rho_1 \\ \beta_1 \\ \alpha_1 \end{pmatrix} \quad \theta_2 = \begin{pmatrix} \rho_2 \\ \beta_2 \\ \alpha_2 \end{pmatrix}$$

Where, ρ_1 and ρ_2 are scalar terms. β_1 and β_2 have the same dimensions as v_t , and α_1 and α_2 are k-vectors. Thus (ρ_1, ρ_2) are the slope coefficients on r_{t-1} , (β_1, β_2) are the slopes on the deterministic components, and (α_1, α_2) are the slope coefficients on $(\Delta r_{t-1}, \dots, \Delta r_{t-k})$ in the two regimes. The threshold effect in Equation 1 has the null hypothesis $H_0: \theta_1 = \theta_2$, which is tested using the familiar Wald statistic:

 $W_T=W_T(\hat{\lambda})=\sup_{\lambda\in\Lambda}W_T(\lambda)$. The stationarity of the

process r_l can be established in two ways. First, when there is a unit root in both regimes. Here the null hypothesis is of the form $H_0: \rho_1 = \rho_2 = 0$, which is tested against the unrestricted

alternative $ho_1
eq 0$ or $ho_2
eq 0$ using the Wald statistic. The

parameters ρ_1 and ρ_2 of Equation 1 control the regime-dependent unit root process of the RER. If $\rho_1=\rho_2=0$ holds,

dependent unit root process of the RER. If $\rho_1 = \rho_2 = 0$ holds, the RER has a unit root can be described as a rejection of PPP. This statistic is:

$$R_{2T} = t_1^2 + t_2^2 (2)$$

Where, t_1 and t_2 are the t ratios for $\hat{\rho}_1$ and $\hat{\rho}_2$ from the ordinary least squares estimation. However, Caner and Hansen(2001) claim that this two-sided Wald statistic may have less power than a one side version of the test. As a result, they propose the following one-side Wald statistic as follows:

Table 1. Univariate unit root test for real exchange ra

Country	ADF	PP	KPSS
Algeria	-1.374(0)	-1.467[3]	1.445[15]***
Botswana	-1.312(0)	-1.445[5]	1.419[15]***
Burkina Faso	-1.994(0)	-1.835[11]	0.831[15]***
Burundi	-2.776(1)*	-3.465[8]***	0.302[15]
Cameroon	-1.312(0)	-1.259[5]	0.885[15]***
Côte d'Ivoire	-1.168(0)	-1.145[5]	0.959[15]***
Egypt	-2.267(0)	-2.283[4]	0.839[15]***
Ethiopia	-1.456(0)	-1.582[4]	0.684[15]**
Gambia	-2.174(1)	-2.062[4]	0.364[15]*
Kenya	-0.315(1)	-0.563[5]	1.900[15]***
Madagascar	-1.697(1)	-2.329[11]	0.395[15]*
Malawi	-3.104(0)**	-3.253[2]**	0.310[15]
Mauritius	-0.765(0)	-0.771[1]	1.811[15]***
Morocco	-0.090(0)	-0.047[2]	1.809[15]***
Niger	-2.328(0)	-2.078[7]	0.436[15]*
Nigeria	-1.763(0)	-1.962[6]	0.372[15]*
Senegal	-1.679(0)	-1.656[1]	0.596[15]**
Seychelles	-2.414(0)	-2.324[8]	1.724[15]***
South Africa	-1.984(0)	-2.091[7]	0.748[15]***
Swaziland	-1.903(0)	-1.966[11]	0.994[15]***

^{***} and ** indicate significance at the 0.01 and 0.05 levels, respectively. The number in parenthesis indicates the lag order selected based on the recursive t-statistic, as suggested by Perron (1989). The number in the brackets indicates the truncation for the Bartlett Kernel, as suggested by the Newey and West test (1987).

$$R_{1T} = t_1^2 I_{\hat{\rho}_1 < 0} + t_2^2 I_{\hat{\rho}_1 < 0} \tag{3}$$

 R_{1T} tests H_0 against the one-side alternative $\rho_1 < 0$ or $\rho_2 < 0$. Caner and Hansen (2001) show that both tests R_{1T} and R_{2T} will have power against both alternatives.

DATA AND EMPIRICAL RESULTS

We use monthly data that covers from 1980 to 2008 to apply the Caner and Hansen (2001) threshold unit test in testing the validity of PPP. Since the end of the 1980s and the early 1990s, there were several waves of depreciation of domestic currencies in order to stop the extensive overvaluation of exchanges rate in Africa during the 1970s and the 1980s. This empirical study covers twenty African countries. The price series are based on the consumer price index, and the nominal exchange rates are the end period spot rates relative to the U.S. dollar (domestic price of the U.S. dollar). All data is taken from the International Monetary Fund's International Financial Statistics (IMFIS). For comparison, the univariate unit root tests are first employed to examine the null of a unit root in bilateral real exchange rates for twenty countries that we study. Based on the results from Table 1, there is no question that three univariate unit root tests - the augmented Dickey and Fuller (1981, ADF), the Phillips and Perron (1988) and the Kwiatkowski et al. (1992) tests all failed to reject the null of non-stationary real exchange rates among these eighteen countries except Burundi and Malawi. Our results signified that real exchange rate is a random process. In other words, PPP was not held among these eighteen African countries under this study.Next, we used Wald test W_T to examine whether or not we can reject the linear autoregressive model in favor of a threshold model. The results of Wald test in Table 2, and also reported the bootstrap critical values generated at conventional levels of significance. The bootstrap p-value for threshold variables of the form

 $Z_{t-1} = r_{t-1} - r_{t-m}$ for delay parameters m is ranged from 1 to 12. The parameters m is generally unknown; there is no reason to think the optimal delay parameter will be the same across countries. To circumvent this, Caner and Hansen (2001) suggest making m endogenous by selecting the least squares estimate of m that minimizes the residual variance. This amounts to selecting m at the value that maximizes the W_T statistic. We find that W_T statistic is maximized for Burkina Faso, Burundi, Egypt, Kenya, Madagascar, Mauritius and Seychelles when m=1, for Morocco and Nigeria when m=2, for Côte d'Ivoire, Senegal and Swaziland when m=3, for Niger when m=4, for Ethiopia and Malawi when m=6, for

Table 2. Threshold test.

Country		117	Bootstrap critical values (%)			-	
Country	m	W_{T} -	10	5	1	Bootstrap <i>p</i> -value	Threshold
Algeria	9	33.546	49.274	54.088	72.374	0.480	-0.073
Botswana	7	50.523	40.422	41.437	45.344	0.000	0.085
Burkina Faso	1	35.021	59.856	82.757	92.522	0.440	0.021
Burundi	1	61.213	49.630	53.572	60.989	0.010	0.021
Cameroon	12	32.726	61.069	73.837	122.019	0.570	0.073
Côte d'Ivoire	3	38.716	78.097	85.234	116.472	0.420	0.046
Egypt	1	348.505	58.695	79.555	108.768	0.000	0.004
Ethiopia	6	257.659	92.594	110.974	162.427	0.000	-0.090
Gambia	7	74.588	48.681	63.626	81.507	0.020	-0.088
Kenya	1	50.003	40.729	44.159	54.328	0.020	0.021
Madagascar	1	79.971	59.024	63.758	75.713	0.000	0.034
Malawi	6	94.094	47.975	54.984	87.033	0.010	0.124
Mauritius	1	34.289	41.001	44.110	51.588	0.340	-0.017
Morocco	2	31.001	37.487	38.810	40.880	0.460	-0.011
Niger	4	37.078	55.046	63.802	90.117	0.330	0.039
Nigeria	2	32.228	87.424	131.506	171.213	0.670	0.040
Senegal	3	37.432	65.082	78.501	91.289	0.420	0.043
Seychelles	1	107.738	59.222	66.527	108.786	0.020	0.017
South Africa	12	56.931	41.572	44.930	47.055	0.000	0.100
Swaziland	3	28.083	39.202	40.864	47.292	0.710	0.070

Botswana and Gambia when m=7, for Algeria when m=9, and for Cameroon and South Africa when m=12.

Taken together, these results imply strong statistical evidence against the null hypothesis of linearity at least 5% in ten African countries indicating that simple linear models are inappropriate. Next, we explore the threshold unit root properties of RER based on R_{1T} statistic for each delay parameter m, ranging from 1 to 12, paying particular attention to the results obtained for our preferred model. The R_{1T} test results, together with the bootstrap critical value at the conventional levels of significance and the bootstrap p-value, are reported in Table 3.

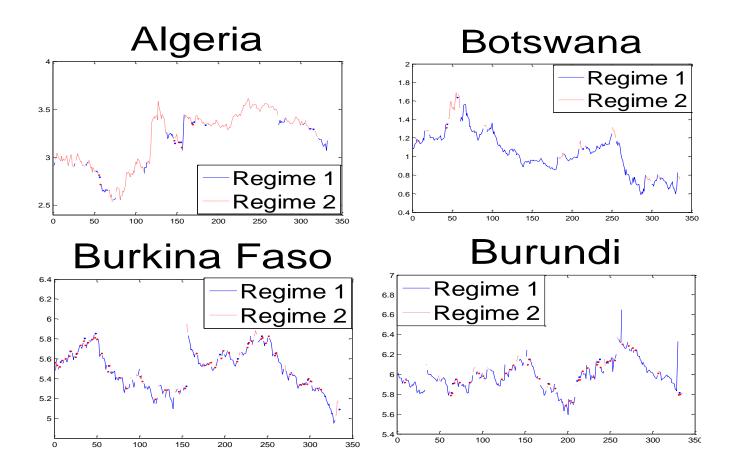
We are able to reject the unit root null hypothesis for Ethiopia and South Africa at the 1% level, for Egypt, Gambia, Malawi and Seychelles at the 5%. However, we are unable to reject the threshold unit root hypothesis for the other fourteen African countries. Taken together, our results provide strong support for PPP for six of twenty African countries and point that these countries are nonlinear stationary, implying that deviations of exchange rate is mean reverting towards the PPP equilibrium. As mentioned earlier, trade barriers, as well as interventions in the exchange markets, could be behind this nonlinear behavior. The validity of PPP is important to policy makers in six African countries who base their determination on exchange rate adjustments. The result means that the unbounded gains from arbitrage in traded goods are impossible among these three countries. Figure 1 shows the estimated division of twenty Africa countries'

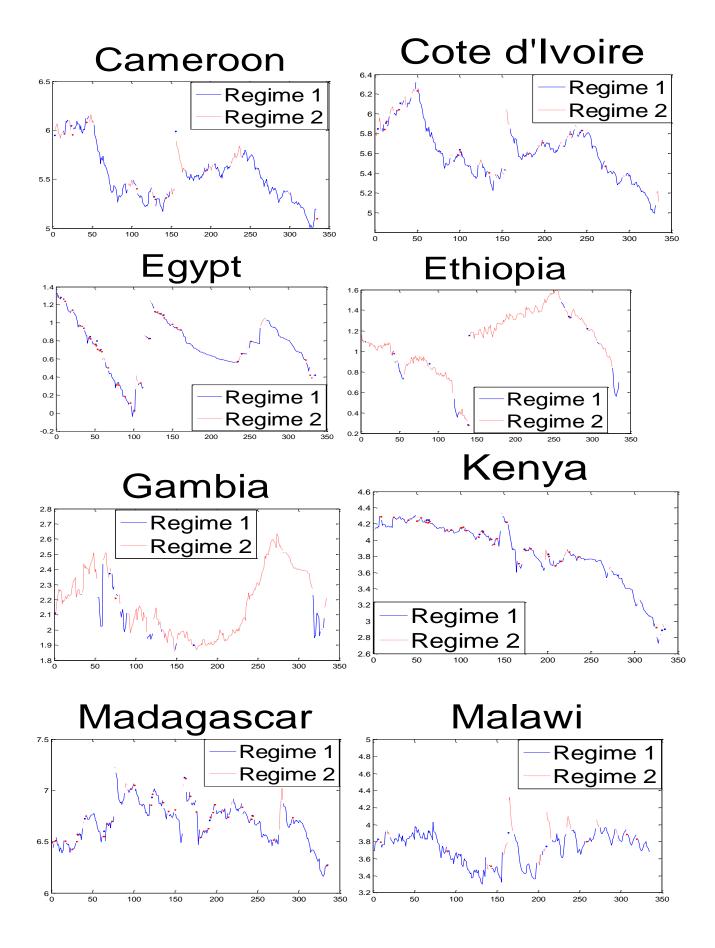
RER into two threshold regimes. The threshold unit root tests of the real exchange rate employed in this study provides some evidence favoring the long-run validity of PPP for the Africa countries being studied. Many of African countries experience double-digit inflation in the last two decades, and the high inflation countries tend to favor the PPP hypothesis. These results clearly qualify the earlier findings of Liu (1992), Mahdavi and Zhou (1994), and others that PPP is most likely to hold in the case of high inflation countries. The major policy implication that emerges from this study is that PPP can be used to determine the equilibrium exchange rate for these six African countries. Our findings are consistent with Holmes (2001) that we can use PPP to predict exchange rate that determine whether a currency is over or undervalued and experiencing difference between domestic and foreign inflation rates. Other countries experienced real shocks, such as droughts, reductions in the terms of trade, oil price shocks, civil wars and other forms of political instability during the past three decades. These problems could trigger destabilizing effects on the PPP relationship in African countries. Periods of political instability are clearly associated with rapid rates of domestic currency depreciation, price increases and inflation in Africa.

Finally, six of African countries RER rates are nonlinearly stationary with their relative price as well as aggregate price levels by the Caner and Hansen (2001) threshold unit root tests that reinforce the validations of

Table 3. Threshold unit root test.

Country	D	Boots	trap critical v		
Country	$R_{_{1T}}$	10	5	1	Bootstrap <i>p</i> -value
Algeria	5.182	9.292	11.087	22.477	0.323
Botswana	6.861	8.409	10.805	16.667	0.170
Burkina Faso	6.421	12.524	18.713	33.213	0.303
Burundi	7.494	12.146	13.404	16.300	0.220
Cameroon	3.451	10.537	13.270	32.688	0.530
Côte d'Ivoire	4.953	11.416	21.165	31.784	0.410
Egypt	20.519	14.138	16.974	36.958	0.050
Ethiopia	39.799	16.311	19.496	27.045	0.010
Gambia	17.298	10.912	15.235	26.556	0.040
Kenya	4.118	8.486	11.305	15.418	0.430
Madagascar	7.292	11.175	17.484	33.718	0.240
Malawi	15.542	9.512	11.345	16.217	0.020
Mauritius	2.701	8.628	10.074	14.324	0.530
Morocco	3.310	8.859	9.777	10.768	0.610
Niger	3.044	13.467	16.450	34.352	0.560
Nigeria	4.948	17.434	20.490	30.883	0.500
Senegal	11.386	12.068	16.966	22.847	0.140
Seychelles	21.742	13.494	16.096	24.467	0.020
South Africa	14.202	7.295	8.622	10.142	0.010
Swaziland	5.016	9.658	12.461	15.183	0.310





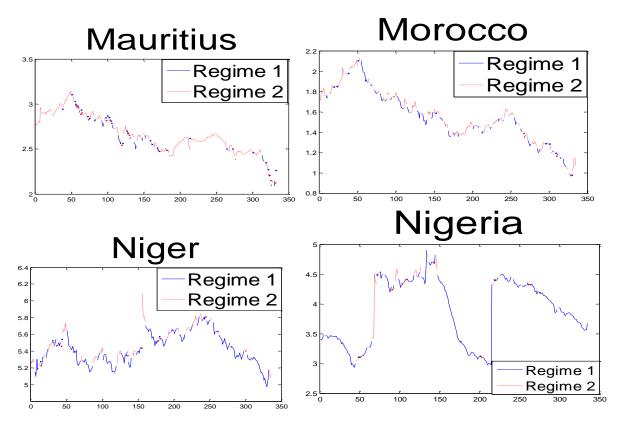


Figure 1. Real exchange rate classified by threshold regime.

long-run PPP using the nonlinear testing procedures. The result means that the governments of these six countries can use PPP to predict exchange rate that determine whether a currency is over or undervalued and experiencing difference between domestic and foreign inflation rates. Nevertheless, reaping unbounded gains from arbitrage in traded goods are impossible among these six countries. The validity of PPP is important to policy makers in African countries who base their determination on exchange rate adjustments.

Conclusion

In this empirical study, we applied non-linear threshold unit-root test to assess the non-stationary properties of the real exchange rate for twenty African countries. The test has higher power than linear method if the true data generating process of exchange rate is in fact a stationary non-liner process. This study examined the validity of PPP from the non-linear point of view and the findings from provide robust empirical evidence supporting the validity of the long-run PPP, suggesting that Egypt, Ethiopia, Gambia, Malawi, Seychelles and South Africa that their real exchange rate adjustment is mean reversion towards PPP equilibrium values in a non-linear way. Because of the wide variability revealed by our

results, the policy formulation process in each African country must reflect the prevailing economic, social and political environment in that country. The other major policy implication of our study is that the validity of using PPP to equilibrium exchange rate and reaping unbounded gains from arbitrage in traded goods is not possible in these six countries.

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