Flat gravity based on Hubble’s law which expanded Newtonian gravity

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Hubble’s law, formulated by Edwin Hubble and Milton Humason in 1929, tells us that space is expanding. However, over short distances, flat gravity caused by the expanding universe is described by the inverse square law of Newtonian gravity. This leads to heretofore unsolved gravity anomalies, such as the pioneer anomaly, which involves an abnormal slowdown relative to the Sun of the Pioneer spacecraft and the galaxy rotation problem, whereby the rotational speed of heavenly bodies reaches a constant value instead of decreasing with distance from the galactic centre. The expanding universe adds an expansion term that was divided into a strain constant \( v = H_0D \) and the gravitational potential \(-GM/(1/r)\) of Newtonian mechanics for a stationary universe is replaced by \(-GM/(1/r+V_0)\). The expansion term becomes constant \((G_0 = GH_0/V_0)\) at large distances because the distance \(D\) and radius \(r\) cancel. Furthermore, the total gravitational mass \([M_0 = cz^2/(2GH_0)]\) of the observable universe affects the specific potential constant, which is multiplied by the observable gravitational mass to become \(-GM/(r+G_0)M\). Flat gravity based on Hubble’s law which expanded Newtonian gravity is thus consistent with the gravity anomaly without assuming the existence of dark matter. When combined with Yukawa potential \([ae^{-r/\lambda} - 1)](G/r + G_0)M\.

Key words: Expanding universe, inverse square law, pioneer anomaly, galaxy rotation problem, recession rate, gravitational potential, stationary universe, gravitational mass, specific potential, dark matter.

INTRODUCTION

Several physical problems in astronomy still remain open. One is the “Pioneer anomaly”, which was noticed for the Pioneer 10 and 11 spacecrafts as they left the solar system. The anomaly involves the cause of the blueshift, which indicates a reduction in speed with respect to the sun and remains unidentified (Anderson et al., 1998). Another open problem is the “galaxy rotation problem” wherein the rotational speed of galactic matter does not decrease with distance from the galactic centre but remains constant (Zwicky, 1933, 1937). Neither of these problems can be explained by Newton’s universal law of gravitation. Some theories have been proposed to revise Newton’s law of gravity, such as modified Newtonian dynamics (MOND), which introduces a function that scales mass and that asymptotically approaches unity for accelerations greater than a constant acceleration defined...
in the theory to be on the order of $10^{-10}$ m/s$^2$ (Milgrom, 1983). Another proposition is the modified gravitation theory (MOG), which expands the theory of general relativity and calls upon a fifth field of force to counteract gravity. However, this theory suggests that, because work becomes small at large distances, gravity must become relatively large, which would require the gravitational constant to change (Brownstein and Moffat, 2006). In addition, the dark-matter hypothesis invokes some unknown “dark” matter (that is, it does not emit radiation) that would account for the observed gravitational anomalies without requiring our current theory of gravity to be modified (Rubin et al., 1980). There is no rationale for the fifth field of force and dark matter remains undiscovered, so the debate is not settled. This paper approaches the problem by assuming an expanding universe, and that a gravitational interaction between all the observable gravitational mass of the universe is the cause of the gravity anomaly. Given this, the spatiotemporal evolution factor from Hubble’s law was first defined (Hubble, 1929) and from this the pioneer anomaly and the galaxy rotation problem was explained.

**METHODS**

Given these relationships, the gravity anomalies by using the specific potential and the equivalence principle of light’s momentum (LEP) was examined.

**Definition of specific potential**

Consider the equation $v = H_0D$, where $v$ is the speed (that is, recession rate) at which heavenly bodies move away from an observer and $D$ is the distance from the observer to the heavenly bodies. The proportionality constant $H_0$ is the Hubble constant and determines the recession rate of the current universe. As of 2013, the most accurate value for the Hubble constant, which comes from the Planck observation, is $67.80 \pm 0.77$ km/s/Mpc (Ade et al., 2013). This recession rate is divided into the recession strain constant $V_0$ (m/s) and is converted into the recession strain $e$ for the cosmic expansion:

$$e = \frac{v}{V_0} = \frac{H_0D}{V_0}. \quad (1)$$

The relationship between the recession strain $e$ and the recession stretch $\Lambda$ is

$$\Lambda = 1 + e = 1 + \frac{H_0D}{V_0}. \quad (2)$$

These equations are expressed by using the ratio of the transformation of the initial state of the spatiotemporal evolution. In addition, we must ask if the recession of galaxies (due to cosmic expansion), and the existence of recession strain and stretch where no expansion occurs are valid before and after unification. Consider the specific potential $G_*$ obtained by multiplying the recession stretch by the gravitational constant and dividing the product by distance:

$$G_* = \frac{AG}{D} = \frac{G}{D} \left( \frac{GH_o}{V_0} \right) m^2 s^{-2} kg^{-1}. \quad (3)$$

The specific potential $G_*$ (J/kg$^2$) multiplied by the active gravitational mass $M_a$ (kg) gives the potential $G_*M_a$ (J/kg). The potential $G_*M_a$ (J/kg) multiplied by the passive gravitational mass $m_p$ (kg) gives the potential energy $G_*M_a m_p$ (J). To obtain the specific potential constant $G_0$, the Hubble constant was multiplied by the gravitational constant and the product divided by the recession-strain constant $V_0$:

$$G_0 = \frac{GH_0}{V_0} m^2 s^{-2} kg^{-1} (J/kg^2). \quad (4)$$

**Kepler’s 3rd law based on LEP**

Centripetal force $F$ to be constant velocity circular motion the inertial mass $m$ is

$$F = m r o^2 = m^2 v^2 / r. \quad (5)$$

By the active gravitational mass $M_a$, and active gravitational mass $m_p$, universal gravitation is

$$F = GM_a m_p / r^2. \quad (6)$$

By using Equations (5) and (6), the equilibrium of forces is:

$$m^2 v^2 / r = GM_a m_p / r^2. \quad (7)$$

By using Equations (7) and using the equivalence principle of light’s momentum (LEP) $v = c /\gamma = m_0 / m$, the equilibrium of potential energies is:

$$m^2 v^2 = G(M_a m_p /r). \quad (8)$$

By using Equations (5) and (8), the equilibrium of potentials is:

$$v^2 = \omega^2 r^2 = G(M_a m_p /r). \quad (9)$$

By using Equations (2) and (9), the equilibrium of potentials in consideration of the recession stretch $\Lambda$ is:

$$v^2 = \omega^2 r^2 = A G(M_a m_p /r). \quad (10)$$

By using Equations (3) and (10) and using $\omega = 2m/\pi T$; Kepler’s 3rd law $r^3 = a T^2$ based on LEP is

$$r^3 = \frac{AG(M_a m_p /r)}{\omega^2} = \frac{AG(M_a m_p /r)}{4\pi^2} T^2$$

$$r^2 = \frac{G_* (M_a m_p /r)}{4\pi^2} T^2 \quad (11)$$

$$r = \frac{\sqrt{G_* (M_a m_p /r)}}{2\pi} T = \frac{v}{\omega}.$$
RESULTS AND DISCUSSION

Pioneer anomaly

Data for short distances (that is, less than 20 au from the Sun) is restored to the original state and is analysed. One report suggests that the anomaly is caused by thermal radiation (Turyshev et al., 2012). Discussion to a base in Figure 1 about it include: Discussion Point A, it thus becomes difficult to explain the Pioneer anomaly by modified gravitation theories, such as MOND or MOG, where gravity or the gravitational constant changes as a function of distance. Discussion Point B, the P10 data at the furthest distance flattened and increased (but within experimental uncertainty) which is inconsistent with a declining thermal cause (Hodge, 2013; Boom, 2013). Discussion Point Other, in addition, it is difficult to envision a solar neighbourhood that does not have dark matter (Bidin et al., 2012) to explain the Pioneer anomaly by the dark-matter hypothesis. As for the major cause of the slowdown, there is no conclusive evidence that the emission of the heat is the cause of the slowdown, nor for other arguments such as the effect of expanding space on photons (Kopeikin, 2012). It is strange that there is no gravity anomaly in the heliosphere, although we have an inexplicable problem, such as the galactic rotation curve, which is based only on the matter that is visible. Furthermore, there is the discussion that insisted on "If the Pioneer anomaly has a gravitational origin, it would, according to the equivalence principle, distort the motions of the planets in the Solar System" Tangen, 2007). However it is an inherent problem of the general relativity based on Weak equivalence principle (WEP) and Einstein's equivalence principle (EEP) "After an illustration by comparing the status of time in Einsteinian physics with that of the vertical direction in Newtonian physics, it was concluded that there is no pertinent notion of time in Einsteinian theories." (Lachieze, 2014, 2007; Mizony and Lachieze, 2005). This paper proposes that the Doppler blueshift that revealed the reduction in Pioneer's speed relative to the Sun is due to flat gravity that is caused by cosmic expansion. The decrease $\Delta v$ in the velocity of the receiver relative to the source with blueshift $\Delta f$ (5.99 ± 0.01 × 10$^{-9}$ Hz) for frequency $f_0$ (2.29 GHz) is:

$$\Delta v = \frac{\Delta f}{f_0} \approx 7.84 \times 10^{-10} \text{ m/s},$$ (12)

which is within the error of $(7.84 \pm 0.01 \times 10^{-8} \text{ cm/s}^2)$ from our formal solution for the Pioneer anomaly that was obtained from the available data (Turyshev and Toth, 2010). The slowdown (escape speed) of Pioneer that is due to flat gravity is calculated from the decrease in wave speed by using Equations (1) and (10) and using the expression $c^2 = w^2 + 2GM$ where $c$ is the speed of light in vacuum and the wave speed in a gravitational field is:

$$2eG(Ms/r')/r = 2G_0(Ms/r') = c^2 - w^2$$

$$= c^2 - (c - \Delta v)^2 = 2c\Delta v - \Delta v^2 \approx 2c\Delta v.$$ (13)

By using Equations (4), (13) and using a solar mass $M_s = 1.989 \times 10^{30}$ kg (Astrodynamic Constants), the specific potential constant is:
Figure 2. Adjusted the rotation curve (red) by Total gravity to Figure 10 (Kafle et al., 2012), and the rotation curve (blue) by Newtonian gravity and the rotation curve (pink) by Flat gravity were added.

\[ G_0 = \frac{G H_0}{V_0} \approx \frac{c \Delta v}{(M_\gamma/r)} \approx 1.18 \times 10^{31} \text{J/kg}^3. \]  \hfill (14)

In Equation (14), the specific potential constant \( G_0 \) is the gravitational mass and a proportionality constant for the blueshift. Transforming Equation (14) gives the recession strain constant \( V_0 \):

\[ V_0 = \frac{G H_0}{G_0} \approx 1.240 \text{ m/s}. \]  \hfill (15)

The ratio of solar mass to total gravitational mass \( M_0 = \frac{c^3}{(2G H_0)} \) of the observable universe (Kragh, 1999) is:

\[ \frac{M_0}{(M_\gamma/r)} = \frac{c^2}{2V_0 \Delta v} \approx 4.62 \times 10^2. \]  \hfill (16)

In addition, the specific potential constant \( G_\alpha \) is a proportionality constant of flat gravity: \( G_\alpha M = Mc^3/(2M_vV_0) \). It acts on gravitational mass and gives the total observable gravitational mass of the universe.

**Galaxy rotation problem**

From Newton’s theory, the galactic rotational speed is:

\[ v_r = \sqrt{G(M_\gamma/r)/r} \text{ m/s}. \]  \hfill (17)

In terms of the specific potential \( G_\alpha \), this is:

\[ v_r = \sqrt{G_\alpha (M_\gamma/r)} = \sqrt{(G/r + G_0)(M_\gamma/r)} \text{ m/s}. \]  \hfill (18)

Therefore, given the galactic rotational speed \( v_r \) and the radius \( r \), we can determine the galactic gravitational mass \( M_\gamma \). This calculation was applied to Figure 2 and 3 of the STELLAR HALO model of the Milky Way galaxy (Kafle et al., 2012) [the Milky Way has an inner and outer halo that]
spreads far and wide. It is in the latter that flat gravity flattens the velocity distribution curve. The curve for dark matter (that is, Halo) and the flat gravity curve are similar, except that a discrepancy emerges for large $r$ (kpc). However, examples such as Abell 520 are observed and indicate that dark matter exists far from the galactic disk and bulge (Mahdavi et al., 2007). Such examples cannot be explained by the conventional dark-matter hypothesis. Because flat gravity extends to an infinite distance, if flat gravity exists, it is indifferent to dark matter (Figure 4).

**Small-scale crisis**

The lambda Cold Dark Matter ($\Lambda$-CDM) model which added the effect (cosmic constant $\Lambda$) of the accelerating expansion of the universe to dark matter = Cold Dark Matter (CDM) which can disregard collisionless damping is a standard model of structure formation. However, as for the $\Lambda$-CDM model, disagreement with observation is pointed out in the small scale (below a Galaxy scale) (D'Onghia and Lake, 2004). Missing satellite problem (Klypin et al., 1999; Moore et al., 1999): Near the Milky Way galaxy (local group of galaxies), tens of dwarf galaxies (satellite galaxy) exist. However, N-body simulation of a $\Lambda$-CDM model is predicting that dark matter halo of about 500 dwarf galaxy mass exists in the same range. This suggests a possibility that the CDM model is wrong. Cuspy halo problem (Blok, 2009): According to the N-body simulation, a center becomes high-density by the very cusp of the density profile of dark matter halo. However, if it asks for a density profile from observation of the rotation curve of a dwarf galaxy, the profile of such a cusp will not be found. There are two huge black-holes in the bulge of the Andromeda Galaxy, and the material density of the central part is not high (Corbelli et al., 2010). Flat gravity and a dark matter curve are in agreement if $r$ (kpc) becomes large (Figure 5). Moreover, the central part does not become high-density like the density profile of CDM. Those problems seem to adjust forcibly by the dark matter hypothesis.

**Large-scale crisis**

The scale of Hercules-Corona Borealis Great Wall is very huge. At the maximum of the size presumed from distribution of the gamma-ray burst, length is 10 billion light years and width is 7,200 million light years (Horvath et al., 2013). In the CDM model, the shock wave which occurred in the universe after the Big-Bang is assumed to be the base which makes the large-scale structure of the present universe. The size of the large-scale structure which arises from it should not exceed about 1,200 million light years (Yadav et al., 2010). This may show that it is unsuitable to predict the homogeneity of the actual universe and formation of large-scale structure by the CDM hypothesis. The Table 1 is the table which summarized the above.
Figure 5. Adjusted the rotation curve (blue) by Newtonian gravity and the rotation curve (pink) by Flat gravity to Figure 14 (Corbelli et al., 2010). The M31 rotation curve (points) and the best fitting mass model (solid line) using the NFW dark halo profile with C = 12 in the frame of CDM. Also shown are the dark halo contribution (dot dashed line), the stellar disk and bulge (short dashed line) and the gas contribution (long dashed line). The bottom panel refers to the case \((M/L)_d = (M/L)_b = 4.2 M/L\). The top panel refers to the best fit when the mass-to-light ratio of the disk and the bulge are two independent variables. For the best fit \((M/L)_d = 5.0\) and an \((M/L)_b = 2.7 M/L\).

Table 1. Summary of this paper.

<table>
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<th>Open problem</th>
<th>Microscopic</th>
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<td>Explanation</td>
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Conclusion

The specific potential constant that was calculated from the abnormal acceleration of the planetary probe pioneer with respect to the Sun is \(G_0 = 1.18 \times 10^{-31} \text{ J/kg}^2\). Given a galactic mass approximately 100 billion times that of the Sun gives a galactic rotational speed of \(v_0 = (G_0 M_\odot /r)^{1/2} = 150 \text{ km/s}\). The gravitational potential is \(-GM(1/r)\) in a static universe; however, the influence of cosmic expansion should be considered in an expanding universe by using \(-GM(1/r)(1 + \text{expansion}) = -(G/r + G_0)M\) for all scales from the microscopic to the large scale of the universe. This resembles the relation between the longitudinal Doppler effect \((1 - v/c)\) and the transverse
Doppler effect \((1 - v^2/c^2)^{1/2}\). Flat gravity can be named longitudinal gravity if Newtonian gravity is named transverse gravity. None of the theories (flat gravity, dark matter or modified gravitation) can explain all scales. However, flat gravity offers the possibility to explain small scales, such as the microscopic scale, which may increase correction term in the Newtonian gravitational potential, and the large scale, such as the intergalactic scale. It is important to gain experience with various scales for the expanding universe because we are familiar with Kepler’s laws and Newtonian mechanics but need more experience with flat gravity. Not only an apple but all the matter in the expanding universe are in the state of free-fall.

**Conflict of Interest**

The author has not declared any conflict of interest.

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