## Full Length Research Paper

# Scheduling of AGVs and machines in FMS with makespan criteria using sheep flock heredity algorithm 

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#### Abstract

This paper addresses the problem of simultaneous scheduling of machines and two identical automated guided vehicles (AGVs) in a flexible manufacturing system (FMS) so as to minimize makespan and mean tardiness. For solving this problem, a sheep flock heredity algorithm is proposed. An increase in the performance of the FMS under consideration would be expected as a result of making the scheduling of AGVs an integral part of the overall scheduling activity. For this particular problem, coding has been developed, which gives optimum sequence with makespan value and AGV'S schedule for ten job sets and four layouts. Most of the time, results of sheep flock algorithm are better than other algorithm and traditional methods.


Key words: Scheduling, AGVs, FMS.

## INTRODUCTION

A flexible manufacturing system (FMS) is a highly automated manufacturing system well suited for the simultaneous production of a wide variety of part types in low to mid volume quantities at a low cost while maintaining a high quality of the finished products.
The increased demand for manufactured goods has increased the pressure on the manufacturing system, which in turn has motivated management to find new ways to increase productivity, considering the scarce available resources.

A flexible manufacturing system (FMS) has emerged as a viable alternative to conventional manufacturing system. Existing FMS implementations have already demonstrated a number of benefits in terms of cost reductions, increased utilizations, reduced work-in-process levels, e.t.c. However, there are a number of problems faced during the life cycle of an FMS. These problems are classified into: design, planning, scheduling and control. In particular, the scheduling task and control problem during the operation is of importance owing to the dynamic nature of FMS such as flexible parts, tools, AGV routings and AS/RS storage assignments. These are primarily concerned with scheduling problems of FMS.

[^0]In FMS scheduling, decisions that need to be made include not only sequencing of jobs on machines but also the routing of the jobs through the system. Apart from the machines, other resources in the system, e.g. materialhandling devices like AGVs and AS/RS must be considered.

AGV is a material handling system that uses independently operated, self-propelled vehicles that are guided along defined pathways in the floor. The vehicles are powered by means of on-board batteries that allow operation for several hours between recharging. The definition of the pathways is generally accomplished using wires embedded in the floor or reflective paint on the floor surface. Guidance is achieved by sensors on the vehicles that can follow the guide wires or paint.
Mean tardiness is useful when the objective function of the company includes a penalty per unit of time if a job completion is delayed a specified due date.

## LITERATURE REVIEW

Sabuncuoglu and Hommertzheim (1992) addressed the simultaneous scheduling problem using a dynamic programming approach. They tested different machines and AGV scheduling rules in FMS against the mean flow time criterion. Another off-line model for simultaneous sche-


Figure 1. Basic model for this particular problem.


Figure 2. The layout configurations used in generating example problems.
duling of machines and material handling system in an FMS for the makespan minimization is presented by Bilge and Ulusoy (1995). The problem was formulated as a non-linear mixed integer-programming model and was addressed using the sliding time window approach. Ulusoy et al. (1997) has addressed the same problem using genetic algorithms. In their approach, the chromosome represents both the operation number and AGV assignment which requires the development of special genetic operators.
Rao and Reddy (2006), addresses the simultaneous scheduling problem as a multi-object problem in scheduling as scheduling with conflicting objectives are more complex and combinatorial in nature. He solved the problem by non-dominating sorting evolutionary algorithm. Wu and Wysk (1988) described some scheduling algorithm which employs discrete simulation in combination with straight forward part dispatching rules in a dynamic fashion.

## METHODOLOGY

In this study, a flexible manufacturing system (FMS) in which material transfer between machines is performed by a number of identical automated guided vehicles (AGVs) is considered, and the problem of simultaneous scheduling of machines and AGVs is addressed. We have considered 4 different layouts and 10 job sets consisting of $1-8$ different job sets and operations on machines to be performed. The problem is formulated as a nonlinear mixed integer
programming model. Its objective is makespan minimization. The formulation consists of constraint sets of a machine scheduling sub problem and a vehicle scheduling sub problem which interact through a set of sheep flock heredity algorithm constraints for the material handling trip starting times. An iterative procedure is developed where, at each iteration, a new machine schedule is generated by a sheep flock heredity algorithm procedure. The Basic model for this particular problem is explained in Figure 1.

## Algorithm used

The algorithm applied for the present study is the sheep flock heredity algorithm. It is found that the proposed algorithm referred to as the multi-stage genetic operation can find better solutions than those of the simple genetic algorithm through thermal generator maintenance scheduling examples. For example, each sub-chromosome represents the operational schedule of one machine for several consecutive years, and a whole chromosome presents the operational schedule of multiple machines for multiple years. So as to cope with this kind of special string structure, hierarchical genetic operations (crossover and mutation) are introduced. They are; (1) sub-chromosome level genetic operation and; (2) chro-mosome (global) level genetic operation.
Sheep algorithm is used because of the following;

- It is a multi-stage genetic operation, can find better solutions than those of the simple genetic algorithm.
- Algorithm shows reasonable combination of local and global search.
- The method is effectively applied to planning problems for multiple years, and the method is tested by the real scale generator maintenance scheduling problem.


## FMS description

The FMS considered in this work has the configuration as shown in Figure 2. There are four machines having computer numerical machines (CNCs), each with an independent and self sufficient tool magazine, one automatic tool changer (ATC) and one automatic pallet changer (APC).

## Assumptions

The types and number of machines are known, there is sufficient input/output buffer space for each machine's machine loading allocation of tools to machine assignment of operation to machine are made pallet and other necessary equipment are allocated. The speed of AGV ( $40 \mathrm{~m} / \mathrm{min}$ ), the distance between the two machines and the distance between loading/ unloading machines are known.

## Input data

The input data that is, traveling time matrix from Table 1 and job sets for the problem is taken from Bilge and Ulusoy (1995). Data given in Table 1 gives the distances from load/unload stations to machines and distances between machines in metres for all the 4 layouts. The 10 job sets given each containing four to eight different job sets, machines in each job set to be processed and numbers within the parenthesis is the processing time of a particular job on a specified machine. The load/unload (LIU) station serves as a distribution center for parts not yet processed and as a collection center for parts finished. All vehicles start from the LIU station initially.

Table 1. Travel time matrix for this particular problem

| Layout 1 | L/U | M1 | M2 | M3 | M4 |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | L/U | 0 | 6 | 8 | 10 | 12 |
|  | M1 | 12 | 0 | 6 | 8 | 10 |
|  | M2 | 10 | 6 | 0 | 6 | 8 |
|  | M3 | 8 | 8 | 6 | 0 | 6 |
|  | M4 | 6 | 10 | 8 | 6 | 0 |
|  | Layout 2 | L/U | M1 | M2 | M3 | M4 |
|  | 0 | 4 | 6 | 8 | 6 |  |
|  | M1 | 6 | 0 | 2 | 4 | 2 |
|  | M2 | 8 | 12 | 0 | 2 | 4 |
|  | M3 | 6 | 10 | 12 | 10 | 2 |
|  | M4 | 4 | 8 | 10 | 12 | 0 |
|  | Layout 3 | L/U | M1 | M2 | M3 | M4 |
|  | 0 | 2 | 4 | 10 | 12 |  |
|  | M1 | 12 | 0 | 2 | 8 | 10 |
|  | M2 | 10 | 12 | 0 | 6 | 8 |
|  | M3 | 4 | 6 | 8 | 0 | 2 |
|  | M4 | 2 | 4 | 6 | 12 | 0 |
|  | Layout 4 | 0 | M1 | M2 | M3 | M4 |
|  | L/U | 18 | 0 | 8 | 10 | 14 |
|  | M1 | 20 | 14 | 4 | 6 | 10 |
|  | M2 | 12 | 8 | 0 | 8 | 6 |
|  | M4 | 14 | 14 | 0 | 0 | 6 |
|  |  |  |  |  | 6 | 0 |

## Data for the job sets used in example problems

## Job Set 1

Job 1: MI(8); M2(16); M4(12)
Job 2: MI(20); M3(10); M2(18)
Job 3: M3(12); M4(8); MI(15)
Job 4: M4(14); M2(18)
Job 5: M3(10); MI(15)

## Job Set 2

Job 1: MI(10); M4(18)
Job 2: M2(10); M4(18)
Job 3: Ml(10); M3(20);
Job 4: M2(10); M3(15); M4(12)
Job 5: Ml(10); M2(15); M4(12); M4(17)
Job 6: MI(10); M2(15); M3(12)

## Job Set 3

Job 1: MI(16); M3(15)
Job 2: M2(18); M4(15)
Job 3: M1(20); M2(10)
Job 4: M3(15); M4(10)
Job 5: MI(8); M2(10); ); M3(15);
Job 6: M2(10); M3(15); M4(8);

## Job Set 4

Job 1: M4(11); MI(10); M2(7)
Job 2: M3(12); M2(10); M4(8)
Job 3: M2(7); M3(10); Ml(9); M3(8)
Job 4: M2(7); M4(8); Ml(12); M2(6)

Job 5: MI(9); M2(7); M4(8); M2(10); M3(8)

## Job Set 5

Job 1: MI(6); M2(12); M4(9)
Job 2: MI(18); M3(6); M2(15)
Job 3: M3(9); M4(3); MI(12)
Job 4: M4(6); M2(15)
Job 5: M3(3); MI(9)

## Job Set 6

Job 1: MI(9); M2(11); M4(7)
Job 2: MI(19); M2(20); M4(13)
Job 3: M2(14); M3(20); M4(9)
Job 4: M2(14); M3(20); M4(9)
Job 5: MI(11); M3(16); M4(8)
Job 6: Ml(10); M3(12); M4(10)

## Job Set 7

Job 1: MI(6); M4(6)
Job 2: M2(11); M4(9)
Job 3: M2(9); M4(7)
Job 4: M3(16); M4(7)
Job 5: MI(9); M3(18)
Job 6: M2(13); M3(19); M4(6)
Job 7: MI(10); M2(9); M3(13)
Job 8: MI(11); M2(9); M4(8)

## Job Set 8

Job 1: M2(12); M3(21); M4(11); M4(6)


Figure 3. Flocks of sheep in a field.


Figure 4. Mix of two flocks of sheep.


Figure 5. New flock of sheep in field.

Job 2: M2(12); M3(21); M4(11)
Job 3: M2(12); M3(21); M4(11)
Job 4: M2(12); M3(21); M4(11)
Job 5: MI(10); M2(14); M3(18); M4(9)
Job 6: MI(10); M2(14); M3(18); M4(9)

## Job Set 9

```
Job 1: M3(9); Ml(12); M2(9);
Job 2: M3(16); M2(11); M4(9)
Job 3: Ml(21); M2(18); M4(7)
```

Job 4: M2(20); M3(22); M4(11)
Job 5: M3(14); Ml(16); M2(13)

## Job Set 10

Job 1: Ml(11); M3(19); M2(16); M4(13)
Job 2: M2(21); M3(16); M4(14)
Job 3: M3(8); M2(10); Ml(14); M4(9)
Job 4: M2(13); M3(20); M4(10)
Job 5: MI(9); M3(16); M4(18)
Job 6: M2(19); MI(21); M3(11); M4(15)

## Objective function

Operation completion time $=\mathrm{Oij}=\mathrm{Tij}+\mathrm{Pij}$; where $\mathrm{j}=$ operation' $\mathrm{i}=\mathrm{job}$, $\mathrm{T} \mathrm{ij}=$ traveling time, $\mathrm{Pij}=$ operation processing time.
Mean tardiness $=\frac{1}{n} \sum_{i=1}^{n} T_{i}$; where $\mathrm{n}=$ number of jobs; $\mathrm{Ti}=$ tardiness.

Optimization parameters considered
Population size $=10$, iterations completed= 1000.

## SHEEP FLOCK HEREDITY ALGORITHM

## Introduction

Sheep flock algorithm was developed by Hyunchul and Byungchul (2001). Consider the several separated flocks of sheep in a field as shown in Figure 3. Normally, sheep in each flock are living within their own flock under the control of shepherds. So, the genetic inheritance only occurs within the flock. In other words, some special characteristics in one flock develop only within the flock by heredity, and the sheep with high fitness characteristics to their environment breed in the flock

In such a world, let us assume that two sheep flocks were occasionally mixed in a moment when shepherds looked aside as shown in Figure 4.Then, shepherd of the corresponding flocks run into the mixed flock, and separate the sheep as before. However, shepherds can not distinguish their originally owned sheep because the appearance of any sheep is the same. Therefore, several sheep of one flock are inevitably mixed with the other flocks as shown in Figure 5, namely, the characteristics of the sheep in the neighboring flocks can be inherent to the sheep in other flocks in this occasion. Then, in the field, the flock of the sheep which has better fitness characteristics to the field environment breeds most.
The above natural evolution phenomenon of sheep flocks can be corresponded to the genetic operations of this type of string. For this kind of string, we can define the following two kinds of genetic operations:

- Normal genetic operations between strings as shown in Figure 7,
- Genetic operations between sub-strings within one string as shown in Figure 8.

We will refer to this type of genetic operation to "multi-stage genetic operation".
GA string can be divided into several sub-strings, and a length of each sub-string is the same. Then, we have the string structure as shown in Figure 6. Figure 6a shows the string structure when it is expanded and Figure 6b shows the same string when it is folded up

(a) String structure(expanded)

(b) String structure(folded)

Figure 6. String structure.


Figure 7. Genetic operations between strings.
in sub-string by sub-string.
Figure 7 shows the genetic operations between strings and Figure 8 shows genetic operations between sub-strings. Let us consider the one to one correspondence of the elements of both actions as shown in Table 2. Then, the inherence within one flock of sheep can be considered as the sub-chromosome level crossover, and the mixing and separating flocks can be corresponded to the chromosome level crossover of the multi-stage genetic operation.

## Steps in sheep flock heredity algorithm

- Initial population is generated randomly.
- For each chromosome, evaluate the desired optimization fitness function.
- Do the sub chromosome level crossover and mutation.
- After selecting the best chromosome from the population do the chromosome level crossover and mutatation.
- The fitness function is calculated for each chromosome in the population. Then do the sorting function. After sorting the strings, the new population is cut down to the size of the old population and this completes one generation of genetic process.
- Loop to step (2) until a termination criterion is met, usually a sufficiently good fitness or a specified number of generations


## Implementation of sheep flock heredity algorithm

The sheep flock heredity algorithm is implemented for optimizing the sequences of parts into the machines, the AGVs sequence for the problem. A new evolutionary computation algorithm based on Sheep flock heredity is proposed. The algorithm simulates heredity of sheep flocks in a prairie. Algorithm is developed for solving a large scale scheduling problem for a period of several successive years. The multi operative mechanisms of sheep flock are very efficient from a computational standpoint. The sheep flock algorithm


Figure 8. Genetic operations between sub-strings.
was built on the following principles;

- Sub chromosomal crossover
- First stage mutation
- Chromosomal crossover
- Second stage mutation

For implementation of sheep flock algorithm, I have considered Job set 5 and Layout 1.

## Job set 5

| Job 1 | Job 2 | Job 3 | Job 4 | Job 5 |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\mathrm{M}_{4} \mathrm{M}_{2}$ | $M_{3} \quad M_{1}$ |
| 123 | 456 | 788 | 1011 | 1213 |

In sheep flock algorithm, first continuous numbers are marked initially for the operations in a job set then random sequence of population ten is generated by following precedence relation that is, operation of the same job set must be in increasing order but anywhere in the sequence.

| 7 | 45 | 118 | 96 | 1012 | 1113 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Job | Machine | AGV | travel time | job reach | job ready job completion |  |  |
| 3,1 | 3 | 1 | 0.00 | 10.00 | 10.00 | 19 |  |
| 2,1 | 1 | 2 | 0.00 | 6.00 | 6.00 | 24 |  |
| 2,2 | 3 | 2 | 24.00 | 8.00 | 32.00 | 38 |  |
| 1,1 | 1 | 1 | 18.00 | 6.00 | 24.00 | 30 |  |
| 3,2 | 4 | 1 | 32.00 | 6.00 | 38.00 | 41 |  |
| 3,3, | 1 | 1 | 41.00 | 10.00 | 51.00 | 63 |  |
| 2,3 | 2 | 2 | 38.00 | 6.00 | 44.00 | 59 |  |
| 4,1 | 4 | 2 | 54.00 | 12.00 | 66.00 | 72 |  |
| 5,1 | 3 | 1 | 63.00 | 10.00 | 73.00 | 76 |  |
| 4,2 | 2 | 2 | 72.00 | 8.00 | 80.00 | 95 |  |
| 5,2 | 1 | 1 | 76.00 | 8.00 | 84.00 | 93 |  |
| 1,2 | 2 | 2 | 86.00 | 6.00 | 95.00 | 07 |  |
| 1,3 | 4 | 2 | 104.00 | 8.00 | 112.00 | 121 |  |
| Maximum job completion time: 121 |  |  |  |  |  |  |  |

placed at different fix points. Then the COF for the mutated sequences is found out, if the COF values are lower than the initial string, then the new string is replaced in place of the initial one, else the initial chromosome is retained.


Table 2. Correspondence of the elements.

| Natural evolution | Multi stage genetic operation |
| :--- | :--- |
| Flock | String |
| Sheep | Sub-string |
| Mixed and separated | Chromosome level crossover |
| Inheritance within flock | Sub-chromosome level crossover |


| 14710 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | $\frac{12 \quad 5}{2}$ | $\frac{811 \quad 13}{3}$ | $\frac{3 \quad 9}{4}$ |

subchromosomal crossover

| $12 \quad 2 \quad 5$ | $\frac{1}{2}$ | 4 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Repair function

A repair function is developed that validates chromosomes with any precedence violations. Although some problem specific heuristics are incorporated, the repair function is not designed to be too smart to prevent overly good repairs that lead to high performing children from poorly performing parents. When repairing, care is taken not to create other infeasibilities. Repair is used only to validate offspring generated by operation swap mutation.

Find positions of the operations which violate the precedence relations; If the distance in-between is smaller than half the chromosome length then swap violating operations else choose one of the operations randomly; take it out and reinsert it right before/ after the other one depending $m$ the precedence relations.

## First stage mutation

Inverse mutation: For a sequence s, let i and $j$ be randomly selected two positions in the sequences. A neighbor of $s$ is obtained by inversing the sequence of jobs between i and j positions. If the COF value of the mutated sequence (after inverse mutation) is smaller than that of the original sequence (a generated clone from an antibody), then the mutated one is stored in place of the original one. Otherwise, the sequence will be mutated again with random pair wise interchange mutation.


Pair wise interchange mutation: Given a sequence $s$, let $i$ and $j$ be randomly selected two positions in the sequence s. A neighbor of $s$ is obtained by interchanging the jobs in positions $i$ and $j$. If the COF value of the mutated sequence (after pair wise interchange mutation) is smaller than that of the original sequence, then store the mutated one in place of the original one. In the case where the algorithm could not find a better sequence after the two-mutation procedure, then it stores the original sequence (generated clone).

```
12
First Pos=5 Second Pos=9
12
After repair:
12
```

Chromosomal crossover: After the sub chromosomal crossovers and mutations, the obtained chromosomes are crossovered again by means of chromosomal crossover in which the best five chromosomes which have got the best COF values were chosen and ten new population is generated by means of crossing the chromosomes with the randomly chosen chromosome.

Width $=5$


## Second stage mutation

Then again, the obtained chromosomes are muted with inverse and pair wise interchange mutations chromosomes after inverse and pairwise mutations thus;

Inverse mutation:

```
4
START=3 END =8
4
After repair
4
```

Pair wise mutation:
First Pos $=2$ Second Pos $=9$

## RESULTS AND DISCUSSION

10 different job sets with different processing sequences, and process times are generated and presented. Different combinations of these 10 job sets and 4 layouts are used to generate 82 example problems. In all these problems there are 2 vehicles. Table 3 consists of problems whose $\mathrm{t}_{\mathrm{i}} / \mathrm{p}_{\mathrm{i}}$ ratios are greater than 0.25 while Table 4 consists of problems whose $\mathrm{t}_{\mathrm{i}} / \mathrm{p}_{\mathrm{i}}$ ratios are lesser than 0.25 .

A code is used to designate the example problems which are given in the first column. The digits that follow EX indicate the job set and the layout. In Table 4 another digit is appended to the code. Here, having a 0 or 1 as the last digit implies that the process times are doubled or tripled, respectively, where in both cases travel times are halved.

The problems in Tables 3 and 4 are sorted according to their layouts. Looking closer in Table 3, one can observe

Table 3. Results comparison for $t / p$ ratio $>0.25$.

| Prob No | STW | UGA | AGA | PGA | SFHA |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | [6] | [44] | [1] | [34] |  |
| EX11 | 96 | 96 | 96 | 96 | 90 |
| EX21 | 105 | 104 | 102 | 100 | 96 |
| EX31 | 105 | 105 | 99 | 99 | 105 |
| EX41 | 118 | 116 | 112 | 112 | 119 |
| EX51 | 89 | 87 | 87 | 87 | 87 |
| EX61 | 120 | 121 | 118 | 118 | 118 |
| EX71 | 119 | 118 | 115 | 111 | 128 |
| EX81 | 161 | 152 | 161 | 161 | 137 |
| EX91 | 120 | 117 | 118 | 116 | 111 |
| EX101 | 153 | 150 | 147 | 147 | 148 |
| EX12 | 82 | 82 | 82 | 82 | 80 |
| EX22 | 80 | 76 | 76 | 76 | 76 |
| EX32 | 88 | 85 | 85 | 85 | 74 |
| EX42 | 93 | 88 | 88 | 67 | 96 |
| EX52 | 69 | 69 | 69 | 69 | 72 |
| EX62 | 100 | 98 | 98 | 98 | 86 |
| EX72 | 90 | 85 | 79 | 79 | 87 |
| EX82 | 151 | 142 | 151 | 151 | 128 |
| EX92 | 104 | 102 | 104 | 102 | 93 |
| EX102 | 139 | 137 | 136 | 135 | 130 |
| EX13 | 84 | 84 | 84 | 84 | 80 |
| EX23 | 86 | 86 | 86 | 86 | 80 |
| EX33 | 86 | 86 | 86 | 86 | 79 |
| EX43 | 95 | 91 | 89 | 89 | 92 |
| EX53 | 76 | 75 | 74 | 74 | 73 |
| EX63 | 104 | 104 | 104 | 103 | 86 |
| EX73 | 91 | 88 | 86 | 83 | 94 |
| EX83 | 153 | 143 | 153 | 153 | 130 |
| EX93 | 110 | 105 | 106 | 105 | 94 |
| EX103 | 143 | 143 | 141 | 139 | 127 |
| EX14 | 108 | 103 | 103 | 103 | 101 |
| EX24 | 116 | 113 | 108 | 108 | 113 |
| EX34 | 116 | 113 | 111 | 111 | 115 |
| EX 44 | 126 | 126 | 126 | 126 | 130 |
| EX 54 | 99 | 97 | 96 | 96 | 96 |
| EX 64 | 120 | 123 | 120 | 120 | 125 |
| EX 74 | 136 | 128 | 127 | 126 | 145 |
| EX 84 | 163 | 163 | 163 | 163 | 146 |
| EX 94 | 125 | 123 | 122 | 122 | 126 |
| EX 104 | 171 | 164 | 159 | 158 | 173 |

STM- Sliding time window; AGA- Abdelmaguid genetic algorithm; UGA- Ulusoy genetic algorithm; PGA-Proposed genetic algorithm; t - travelling time; p - processing time.
that, while high improvements are achieved on layouts 2 and 3 , improvements obtained on layouts 1 and 4 are less. The following steps are used to calculate the mean tardiness of the sheep flock heredity algorithm:

Repair Function: ${ }^{13} / 2=6.5$
$\left.\begin{array}{llllllllllll}12 & 1 & 4 & 2 & 5 & 7 & 10 & 8 & 11 & 13 & 3 & 6\end{array}\right)$

Step 1: Calculating the average value of makespan by using the relation
$\left(\mathrm{C}_{1}+\mathrm{C}_{2}+\ldots \ldots \ldots+\mathrm{C}_{\mathrm{n}}\right) / \mathrm{n}$
where; $\mathrm{C}_{1}, \mathrm{C}_{2}, \ldots . . \mathrm{C}_{\mathrm{n}}=$ first layout make span values of n job sets

Table 4. Results comparison for $\mathrm{t} / \mathrm{p}$ ratio $<0.25$.

| Prob No | STW | UGA | AGA | PGA | SFHA |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | [6] | [44] | [1] | [34] |  |
| EX110 | 126 | 126 | 126 | 126 | 119 |
| EX210 | 148 | 148 | 148 | 148 | 128 |
| EX310 | 150 | 148 | 150 | 150 | 128 |
| EX410 | 121 | 119 | 119 | 119 | 112 |
| EX510 | 102 | 102 | 102 | 102 | 100 |
| EX610 | 186 | 186 | 186 | 186 | 143 |
| EX710 | 137 | 137 | 137 | 137 | 137 |
| EX810 | 292 | 271 | 292 | 292 | 247 |
| EX910 | 176 | 176 | 176 | 176 | 185 |
| EX1010 | 238 | 236 | 238 | 238 | 123 |
| EX120 | 123 | 123 | 123 | 123 | 132 |
| EX220 | 143 | 143 | 143 | 114 | 111 |
| EX320 | 148 | 145 | 145 | 100 | 97 |
| EX420 | 116 | 114 | 114 | 114 | 140 |
| EX520 | 100 | 100 | 100 | 100 | 136 |
| EX620 | 183 | 181 | 181 | 181 | 244 |
| EX720 | 136 | 136 | 136 | 136 | 155 |
| EX820 | 287 | 268 | 287 | 287 | 184 |
| EX920 | 174 | 173 | 173 | 173 | 118 |
| EX1020 | 236 | 238 | 236 | 236 | 126 |
| EX130 | 122 | 122 | 122 | 122 | 136 |
| EX230 | 146 | 146 | 146 | 146 | 110 |
| EX330 | 149 | 146 | 146 | 146 | 93 |
| EX430 | 116 | 114 | 99 | 99 | 110 |
| EX530 | 99 | 99 | 182 | 182 | 93 |
| EX630 | 184 | 182 | 137 | 137 | 142 |
| EX730 | 137 | 137 | 288 | 288 | 137 |
| EX830 | 288 | 270 | 174 | 174 | 245 |
| EX930 | 176 | 174 | 237 | 237 | 161 |
| EX1030 | 237 | 241 | 124 | 124 | 185 |
| EX140 | 124 | 124 | 217 | 217 | 118 |
| EX241 | 217 | 217 | 151 | 151 | 187 |
| EX340 | 151 | 151 | 221 | 221 | 136 |
| EX 341 | 222 | 221 | 172 | 172 | 185 |
| EX 441 | 179 | 172 | 148 | 148 | 166 |
| EX 541 | 154 | 148 | 184 | 184 | 137 |
| EX 640 | 185 | 184 | 137 | 137 | 161 |
| EX 740 | 138 | 137 | 203 | 203 | 137 |
| EX 741 | 203 | 203 | 293 | 293 | 203 |
| EX 840 | 293 | 273 | 175 | 175 | 268 |
| EX940 | 177 | 175 | 240 | 240 | 146 |
| EX1040 | 240 | 244 | 175 | 175 | 185 |

$\mathrm{n}=$ number of job sets
Step 2: Find out the due date (Di).
Here average makespan values are considered as Di.
Step 3: Calculating the lateness value (Li)
$\mathrm{Li}=$ makespan - due date
Step 4: Finding out tardiness value (Ti)
$\mathrm{Ti}=\mathrm{Max}(\mathrm{Li}, 0)$
Step 5: Calculating the mean tardiness value $(\bar{T})$

Table 5. Mean makespan and tardiness comparison for $\mathrm{t} / \mathrm{p}$ ratio>0.25.

| Layout | STW |  | UGA |  | AGA |  | PGA |  | SFHA |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness |
| 1 | 118.6 | 8.3 | 116.6 | 7.8 | 115 | 8.4 | 114 | 8.8 | 113 | 8.5 |
| 2 | 99.6 | 9.8 | 96.4 | 9.5 | 96 | 10.5 | 96 | 9.6 | 92 | 7.9 |
| 3 | 102.8 | 10.2 | 100.5 | 9.5 | 100 | 10.4 | 100 | 10 | 93 | 7.3 |
| 4 | 128 | 8.6 | 125.3 | 8.1 | 123 | 8.3 | 123 | 8.1 | 127 | 8.6 |

Table 6. Mean makespan, Mean tardiness comparison for $t / p$ ratio<0.25..

| Layout | STW |  | UGA |  | AGA |  | PGA |  | SFHA |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | Mean <br> make span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness | Mean <br> make <br> span | Mean <br> tardiness |
| 1 | 167 | 22.4 | 164 | 21.3 | 167 | 22.4 | 167 | 22.4 | 145 | 15.4 |
| 2 | 164 | 22.4 | 162 | 21.2 | 163 | 22.5 | 163 | 22.5 | 144 | 15.1 |
| 3 | 165 | 22.5 | 163 | 21.5 | 164 | 22.5 | 164 | 22.5 | 145 | 15.6 |
| 4 | 190 | 18.75 | 187 | 18.58 | 188 | 19.5 | 188 | 19.5 | 169 | 15.25 |

$$
\bar{T}=\frac{1}{n} \sum_{i=1}^{n} T_{i}
$$

## Conclusion and Recommendations

In this paper the optimal sequences of Machines and AGVs are determined. The iterative algorithm created anticipates the complete set of flow requirements for a given machine schedule and makes vehicle assignments accordingly, as opposed to a real-time dispatching scheme that uses no information other than the move request queue. The iterative algorithm promises improvement in scheduling especially in environments where cycle times are short and travel times are comparable, or where the layout and the process routes do not suit each other. Most of the times results of Sheep flock algorithm are better than other algorithm and traditional methods. Out of 40 problems 22 problems give better results using SFHA when compared with other four algorithm and same results for 3 problems. It can also be observed from Table 4 that out of 42 problems, 38 problems give better results using SFHA when compared with other four algorithm and same results for the remaining 4 problems (Table 3). From Table 3 it can be observed that out of 40 problems, 29 give better results using SFHA when compared to the sliding time window (Abdelmaguid et al., 2004) and same results for 1 problem; compared with the Ulusoy genetic algorithm (UGA) (Ulusoy et al., 1997) 25 problems give better results and same results for 3 problems and compared with Abdelmaguid genetic algorithm (AGA) (Abdelmaguid et al., 2004), 20 problems give bet-
ter results and same results for 4 problems.
Optimal and better solutions can be determined within fewer iterations of sheep flock algorithm, when compared with other algorithm in the Tables 3 and 4 respectively. From Tables 5 and 6 we conclude that mean makespan and tardiness values of 4 layouts are better in SFHA (Figures 9 and 10) when compared to other four algorithms. As per Table 5 we conclude that mean makespan and tardiness values of out of 4 layouts, 2 lay outs give better results in SFHA and the other 2 have some variations as compared to the other 4 algorithms. The computational results have indicated that sheep flock algorithm is very effective in generating optimal solutions for FMS. It is possible to adapt the sheep flock heredity algorithm approach to performance criteria other than the makespan, such as the minimization of maximum tardiness and mean flow time. In machine schedule generation, on the other hand, due date related priority rules can be employed in conjunction with active or non delay schedule generators. Problems can be implemented as real time scheduling problem and with necessary additions; traffic control and safety can be incorporated for automated guided vehicle. The number of AGV'S can be increased. Robots and automated storage retrieval system (AS/RS) can be incorporated to this problem.

## LIMITATIONS OF THE WORK

In this particular problem we consider the entire automated guided vehicle as an identical one but in practice that may not be possible. Traffic control, congestion, machine


Figure 9. Comparison chart for $t / p$ ratio $>0.25$.


Figure 10. Comparison chart for $t / p$ ratio $<0.25$.
failure or downtime, scraps, rework and vehicle dispatches for battery changer are ignored here and left as issues to be considered during real-time control. Number of machine considered are 4 which may vary in real time problems and the layout is a simple one.

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