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Full Length Research Paper

A supplement to the Michelson-Morley experiment

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Based on the great Michelson-Morley experiment and predecessors' analyses, this famous experiment was reviewed under the principle that velocity of light is independent of the motion of the light source emitting or reflecting it, mainly on time difference or optical path difference (OPD). We will discover in this work that predecessors' analysis on the famous experiment may be improper, and that there is no difference or OPD in some directions, while there is difference or OPD in other directions after a lot of calculation is done. The light beam is divided into many light rays in the analysis, leading to the research on its effect on the light rays.

Key words: Aether, optical path difference (OPD), Michelson, interferometer, inertia, light, velocity.

INTRODUCTION

With the Michelson interferometer invented by Michelson, one of the most important inventions in the physical history, Michelson and Morley did the famous Michelson-Morley experiment jointly in 1887.

Predecessors' analyses

Let us look at predecessors' analyses on this famous experiment, as shown in Figure 1, where L represents light beam emitting from light source (S) (Mechanics, Tsinghua University Press, Apr 01, 1999; http://galileo.phys.virginia.edu/classes/252/michelson.htm l).

According to predecessors' analyses about the famous experiment, the light beam L travels along the paths in (a) actually and (b) seemingly (Figure 1), where the path in (a) is the expected path of light relative to the aether with an aether wind blowing. In the author's opinion, however, the analyses about the experiment are not quite satisfactory in some aspects. For instance, why does light travel along the path as shown in Figure 1a? This idea may come from the phenomenon - when we throw an apple vertically upwards on running train, the apple will fall back to the exact point before it was thrown off. The people on the train may say the apple moved vertically. However, the people on ground may say the apple actually travelled a slant way, as shown in Figure 1a. The essential difference between apple motion and light travel is that apple is featured by inertia.

In fact, the imagined material which is called aether is

expected to be still in space. The aether wind is actually the effect caused by relative motion of the Earth, and in aether, light will travel along the direction when it is emitted or reflected. Therefore, when the reflected light beam (by G_1) enters aether, the beam will travel along the direction when it is reflected by G_1 – vertically upwards, not slant ways, plus the proven principle that velocity of light is independent of the motion of the light source emitting or reflecting it - light is not featured by inertia.

Why it is considered that light travels along the path (Figure 1a) may be that it seems that the reflected light beam (by G₁) will come back to the exact point on G₁' after the beam is reflected by M₂ during the experiment. Actually, to the author, the reflected light beam (by G₁) is not bound to come back to the exact point on G₁' after the beam is reflected by M2. This is because the reflected light beam (by G₁) will travel vertically upwards and then vertically downwards with G₁ moving all the time. When the light beam reflected by M2 reaches G1', there may exist a little departure [that is, $\sqrt{(2(ut)^2)}$] from the point on G₁' when the beam was reflected. This departure between the reflection point on G₁' and the point when the light beam reflected by M₂ reaches G₁' may be very tiny because of the exceptionally high velocity of light. Therefore, it may be very difficult to observe this departure, leading to the consideration that there is no departure between the two points, as show in Figure 1b. In this way, it seems reasonable to consider that reflected light beam (by G₁) will come back to the exact point on G₁' after the beam is reflected by M₂, where the distance

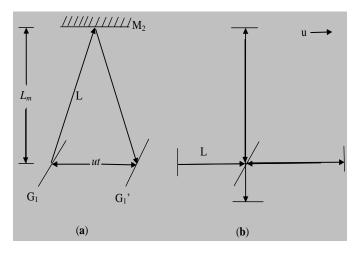


Figure 1. Predecessors' analytical illustrations.

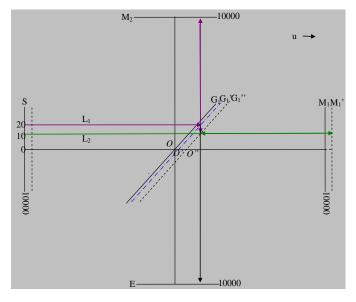


Figure 2. Top light rays which can superpose with each other.

between G_1 and G_1 ' is *ut*, as shown in Figure 1a. This leads to the wrong conclusion that with G_1 moving to G_1 ', the light beam reflected by G_1 must travel along the path as shown in Figure 1a to come back to the reflection point on G_1 ', which lets light to be featured by inertia.

Analysis

Under the principle, we all know that velocity of light is independent of the motion of the light source emitting or reflecting it:

Using the following data (where the unit of time is s, and the unit of length is mm) which may not be quite

accurate:

U

(http://en.wikipedia.org/wiki/Michelson%E2%80%93Morle y_experiment) C = 299792458000 (Waves and Optics, Tsinghua University Press, 2000; Jan 01. http://en.wikipedia.org/wiki/Speed_of_light) c-u = 299762458000 c+u = 299822458000 $SO = OM_1 = OM_2 = OE = 10000$, and the diameter of light beam emitted from S is 40 From Figure 2, the following results can be obtained: T_{SG} (10000+20)/(c-u)=

30000000

 ΔI_1 = OO'= $(T_{11}*c)/(c/u)$ = 1.002794018989529369284795496306 Or, $(10000+20)+\Delta I_1 = (c/u)\Delta I_1$ ΔI_1 =1.002794018989529369284795496306

3.3426467299650978976159849876865e-8

 $\begin{array}{lll} T_{SM1'} &=& (10000^*2)/(c\text{-u}) \\ = &6.6719495608085786379560578596537e\text{-8} \\ D &=& [(T_{SM1'} \, ^*c)/(c/u)]^*2 + 10000^*3 - 20\text{-}\Delta I_1 \\ D &=& \Delta I(c/u) \\ 29983.000375717495617813488839219 &=& \Delta I(c/u) \\ \Delta I &=& 3.0003757174956178134888392194864 &=& OO'' \end{array}$

 $T_{21} = T_{SM1} = (10000^*2)/(c-u) = 6.6719495608085786379560578596537e-8$

 $T_2 = D/c = 1.0001252391652059378296130731618e-7$

 T_{E1} (which is the time L_1 takes to travel from S to E via M_2) = T_{11} + T_{12} + $(10000^*2)/c$ = 1.3342898304005696343891774887643e-7

From the results above, we can find that there is almost no time difference between the 2 superposed light rays, that is, there is almost no OPD between them.

If SO = 3000:

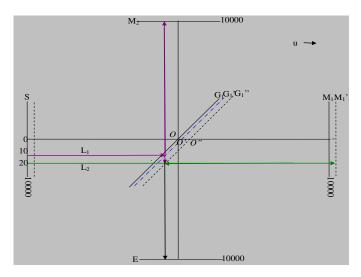


Figure 3. Bottom light rays which can superpose with each other.

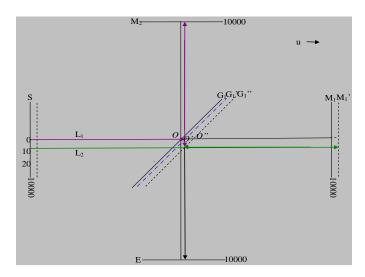


Figure 4. Mid light rays which can superpose with each other.

$$\begin{array}{llll} T_{11} & = & (3000 + 20)/(c - u) & = \\ 1.0074643836820953743313647368077e - 8 & & \\ \Delta I_1 & = & OO' & = & (T_{11} ^*c)/(c/u) & = \\ 0.30223931510462861229940942104232 & & \\ OR, & & & \\ (3000 + 20) + \Delta I_1 = (c/u)\Delta I_1 & & \\ \Delta I_1 = & 0.30223931510462861229940942104232 & & \\ T_{SM1} & = & & (3000 + 10000)/(c - u) & = \\ 4.3367672145255761146714376087749e - 8 & & \\ D = & [(T_{SM1}, ^*c)/(c/u)]^*2 + 3000 + 10000^*2 - 20 - \Delta I_1 & \\ D = & \Delta I(c/u) & & \\ 22982.299821013610717056503453144 = \Delta I(c/u) & \\ \Delta I = 2.2998210136107170565034531442227 = OO'' & & \\ \end{array}$$

 $T_{12} = (10000 -$

```
20)/c=3.3289696700775574547642556104597e-8
              [(10000-20)
                                      (\Delta I)
                                              -\Delta I_1)]/c
3.3296359916094040259158901334747e-8
                        SUM
T₁
                                        (T_{11},
                                                       T_{12},
T_{13})=7.6660700453690568550115104807407e-8
                                (3000+10000)/(c-u)
               T_{SM1}
4.3367672145255761146714376087749e-8
                                    (10000-20-∆I<sub>1</sub>)]/c
             [(T_{21}*c)/(c/u)]
3.3293028308434807403400728719672e-8
T_2
                    SUM
                                 (T_{21},
                                              T_{22})
7.666070045369056855011510480741e-8
T_2 = D/c = 7.6660700453690568550115104807406e-8
The results we obtained above show that there is still
almost no time difference when SO = 3000.
In Figure 3, the following results can be obtained:
                              (10000*2)/(c-u)
6.6719495608085786379560578596537e-8
[(T_{SM1}, *c)/(c/u)]*2+10000*3+20-\Delta I = \Delta I(c/u)
30024.003169736485147182773634716 = \Delta I(c/u+1)
\Delta I = 3.0041782096659835749044629906993 = OO''
(10000-20+\Delta I) = \Delta I_1(c/u)
\Delta I_1 = 0.998991526819163607869171725093
                             (10000-20+\Delta I)/c
3.3299717560638786928972390836432e-8
                        [(10000+20)-(\Delta I-\Delta I_1)]/c
3.3416433756039163533703588729822e-8
                                            (10000+20)/c=
3.3423122338854835367472786790387e-8
                SUM
                           (T_{11},
                                      T<sub>12</sub>,
                                                T_{13})
1.0013927365553278583014876635664e-7
                 T_{SM1}
                                    (10000*2)/(c-u)
6.6719495608085786379560578596537e-8
                                 +(10000+20-\Delta I)I/c
               [(T_{21}*c)/(c/u)]
3.3419778047446999450588187760104e-8
T_2
                    SUM
                                 (T_{21},
                                              T_{22})
1.0013927365553278583014876635663e-7
                                       (10000*2)/c
                 T_{11}+T_{12}
1.3342897035630836037779132246123e-7
In Figure 4, the following results can be obtained:
10000 + \Delta I_1 = \Delta I_1 (c/u)
\Delta I_1 = OO' = 1.0007924341212867956934086789481
                              (10000*2)/(c-u)
```

6.6719495608085786379560578596537e-8

 $D = [(T_{SM1}, *c)/(c/u)]*2+10000*3-\Delta I_1$

 $D = \Delta I(c/u)$

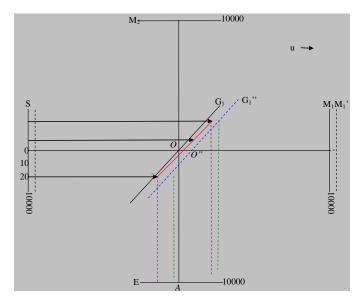


Figure 5. Front section.

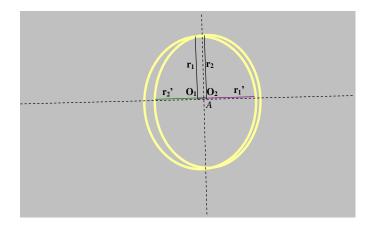


Figure 6. Facula.

 $30003.002377302363860387080226037 = \Delta I(c/u)$ $\Delta I = 3.0023773023638603870802260368442 = OO$

6.6719495608085786379560578596537e-8

$$T_{E1} = T_{11} + T_{12} + (10000^*2)/c = 1.3342897636348850806245330364073e-7$$

Let us compare the 3 ΔI_1 s of the 3 pairs of light rays above (SO = 10000):

$$\Delta I_1$$
 (L_{top}) = 1.002794018989529369284795496306 ΔI_1 (L_{mid}) = 1.0007924341212867956934086789481 ΔI_1 (L_{bot}) = 0.998991526819163607869171725093

By comparing them, we can know that the ΔI_1 s decreases from top to bottom gradually. The rough front section of all light rays when they respectively arrive at G_1 is like the red line in Figure 5.

The final result we will see on view-screen is that the light intensity to the right is higher than that to the left. In Figure 6, r_1 is the radius (in vertical direction) of the facula (on view-screen) of the light beam reflected by M_2 , and r_2 is the radius (in vertical direction) of the facula (on view-screen) of the light beam reflected by M_1 . We can demonstrate that:

 $10000-\Delta I_1=\Delta I_1$ (c/u)

Let us compare the 3 T_{E1} s of the 3 light rays (reflected by M_2) above (SO=10000):

```
\begin{split} T_{E1} \; (L_{top}) &= 1.3342898304005696343891774887643e\text{-}7 \\ T_{E1} \; (L_{mid}) &= 1.3342897636348850806245330364073e\text{-}7 \\ T_{E1} \; (L_{bot}) &= 1.3342897035630836037779132246123e\text{-}7 \end{split}
```

We can find that the light rays (reflected by M_2) to the left arrive at E first. In fact, in Figure 5, we will find that the light rays (reflected by M_2) to the right travel a longer distance than that to the left. Similarly, the light rays (reflected by M_1) to the left arrive at E first.

If u is in the opposite direction (Figure 7), the following results can be obtained:

$$\Delta I_1 = OO' = 1.000592157109191600317011609584$$

$$T_{11} = T_{S0O'} = 10000/(c+u)$$
3.3353071903639720010567053652799e-8
Or,

$$T_{11}$$
 = $(10000-\Delta I_1)/c$ = 3.3353071903639720010567053652799e-8

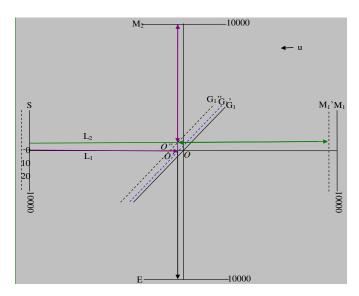


Figure 7. When u is in opposite direction.

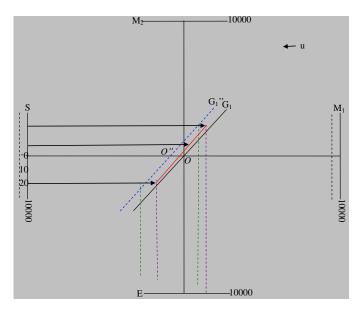
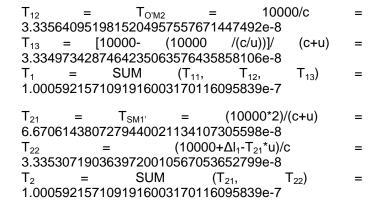


Figure 8. Front section.



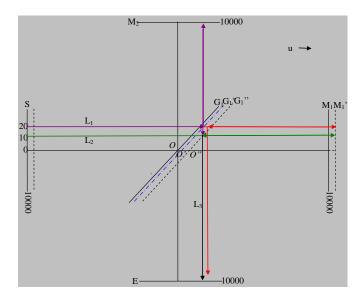


Figure 9. Reflected and transmitted lights.

It is very obvious that there is almost no time difference between the superposed light rays. The final result shows on view-screen light intensity to the right is higher than that to the left, except that the light rays to the right arrive at E first, as shown in Figure 8.

Figure 9 shows that the reflected light ray and transmitted light ray of L1 will not arrive at E at the same time, because L₄ is reflected at one position between G₁' and G₁", rather than at G₁" position. Therefore, L₄ lags behind L₃.

When u is in the direction in Figure 10, it can be demonstrated that there is no OPD between any light rays, and they arrive at E at the same time. The facula is as shown in Figure 11. When u is in the direction as in Figure 12, use the following data:

 $\cos 45^{\circ} = 0.70710678118654752440084436210485$ $\sqrt{(2)} = 1.4142135623730950488016887242097$ $c-u \cos 45^\circ = 299771244796.56440357426797466914$ c+u cos45° = 299813671203.43559642573202533086 $c+\sqrt{(2)}u = 299834884406.87119285146405066173$ $c-\sqrt{2}u = 299750031593.12880714853594933827$ $\sqrt{(2)^*\Delta I_1} = 1.4149923533787645867970063199242$

 $10000 - \sqrt{(2)}\Delta I_1 = \Delta I_1 (c/u)$ $\Delta I_1 = 1.0005506884012360212957595144385$

```
10000/(c+\sqrt{2}u)
3.3351689613374534043191983814616e-8
             (10000+\Delta I_1)
                               cos45°)/(c-u
                                                 cos45°)
3.3361130094260811374539223490032e-8
T_{13}
                       (T_{12}*c-T_{12}*\sqrt{(2)u})/(c+\sqrt{(2)u})
3.3351688945464120728151667032255e-8
\mathsf{T}_1
                 SUM
                             (T_{11},
                                         T<sub>12</sub>,
                                                    T_{13})
1.0006450865309946614588287433689e-7
```

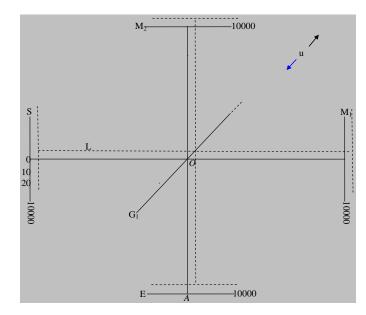


Figure 10. There is no OPD.

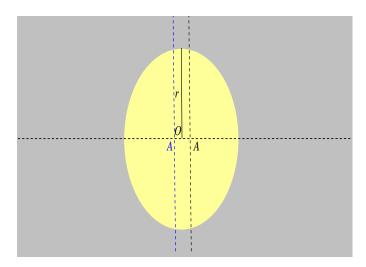
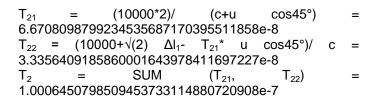


Figure 11. Facula.



$T_1 - T_2 = 6.6800492881473406712772273422988e-16$

We can find in this circumstance there is a time difference or OPD between the superposed light rays. When u is in the direction as in Figure 13:

 $10000 + \sqrt{(2)}\Delta I_1 = \Delta I_1 (c/u)$ $\Delta I_1 = 1.0008339228708088746581223879355$

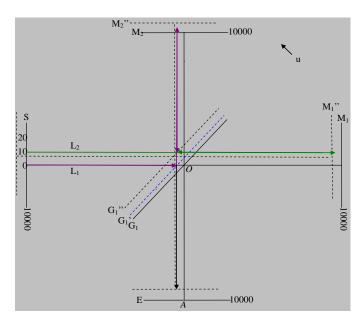


Figure 12. There exists OPD.

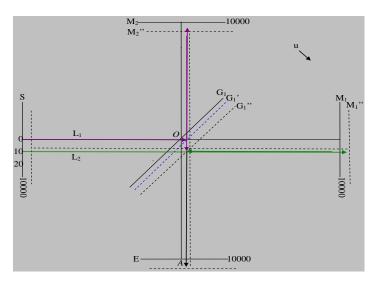


Figure 13. There exists OPD.

```
10000/(c-\sqrt{(2)u})
T_{11}
3.3361130762360295821937412931191e-8
             (10000-\Delta I_1)
                            cos45°)/(c+u
                                              cos45°)
3.3351688945369591850801126030842e-8
                      (T_{12}*c+T_{12}*\sqrt{(2)u})/(c-\sqrt{(2)u})
3.3361130094166255738088173068873e-8
                SUM
                           (T_{11},
                                      T<sub>12</sub>,
                                                 T_{13})
1.000739498018961434108267120309e-7
                (10000*2)/
                                             cos45°)
T_{21}
                                  (c-u
6.6717539948078484083404827142359e-8
T_{22} = (10000 - \sqrt{(2)}\Delta I_1 + T_{21}^* u \cos 45^\circ)/
3.3356410521822608211481468061983e-8
```

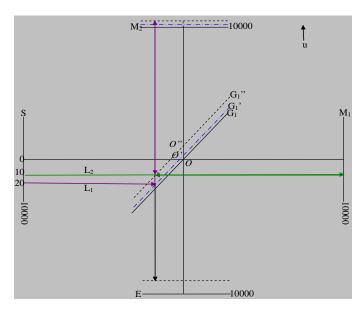


Figure 14. Bottom light rays which can superpose with each other.

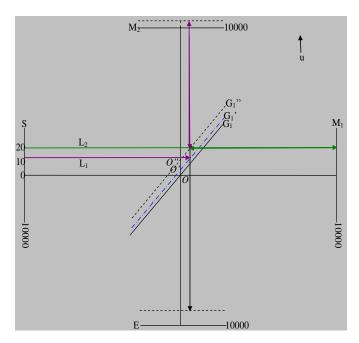


Figure 15. Top light rays which can superpose with each other.

$$T_2$$
 = SUM (T_{21}, T_{22}) = 1.0007395046990109229488629520433e-7

 $T_2 - T_1 = 6.6800494888405958317343320940694e-16$

We can find, in this circumstance, there is a time difference or OPD between the superposed light rays too.

When the direction of u is as shown in Figure 14, the following results can be obtained:

```
(10000-20)-\Delta I_1 = \Delta I_1(c/u)
9980 = \Delta I_1(c/u+1)
\Delta I_1 = 0.99859097279497321711637758636483
                             (10000-20)/(c+u)
3.3286365759832440570545919545493e-8
                          (10000+20+\Delta I_1)/(c-u)
3.3429798573952162392587254463954e-8
                            (T_{12}*c-T_{12}*u)/(c+u)
              =
3.3423108655098795078309698793761e-8
Or
                         (10000+20+\Delta I_1)/(c+u)
3.3423108655098795078309698793765e-8
                SUM
                           (T_{11},
                                                T_{13})
1.001392729888833980414428728032e-7
                          (10000*3+20+\Delta I_1)/c
1.0013927231942837925968476624447e-7
(10000*2)/(c+u)=6.670614380727944002113410730559
8e-8
                       T_{11}+T_{12}+(10000*2)/(c+u)
T_{E1}
1.3342230814106404298426728131503e-7
If SO = 3000:
(3000-20)-\Delta I_1 = \Delta I_1(c/u)
2980 = \Delta I_1(c/u+1)
\Delta I_1 = 0.29817646281853909689446945965603
                             (3000-20)/(c+u)
9.939215427284636563148981988534e-9
                          (10000+20+\Delta I_1)/(c-u)
3.342746200881105177986262198804e-8
                            (T_{12}*c-T_{12}*u)/(c+u)
3.3420772557547435419587196064745e-8
                SUM
                           (T_{11},
                                      T<sub>12</sub>,
                                                T_{13})
7.6787449993643123762598800041288e-8
                      (3000+10000*2+20+\Delta I_1)/c
T_2
7.6787449324234896326500963774945e-8
In Figure 15, the following results can be obtained:
10000*3-20+\Delta I = \Delta I(c/u)
29980 = \Delta I(c/u-1)
\Delta I = 3.0003757174956178134888392194864
Or.
\Delta I = (10000^*2)/(c/u) + [10000-20+(10000^*2)/(c/u)]/(c-u)^*u
            2.0013845711889122974534602868496
0.99899114630670551603537893263674
\Delta I = 3.0003757174956178134888392194857
(10000+20-\Delta I) = \Delta I_1(c/u)
\Delta I_1 = 1.0023934248822067814180813542128
T_{11}
                             (10000+20-\Delta I)/c
3.3413114162740226047269378473759e-8
             [(\Delta I - \Delta I_1)]
                                (10000-20)+\Delta I_1/(c-u)
3.3303037486160110209042550749365e-8
```

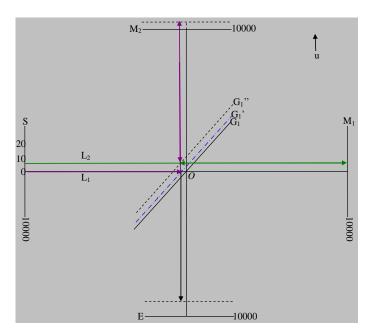


Figure 16. Mid light rays which can superpose with each other.

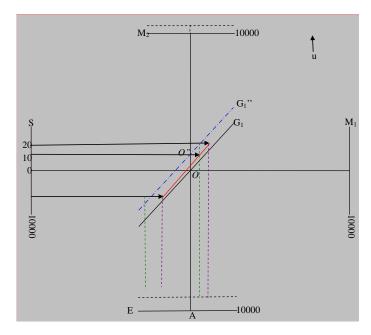


Figure 17. Front section.

 $[(T_{11}+T_{12})^*$

3.3296372934603534989821823195688e-8 $T_1 = SUM (T_{11}, T_{12}, T_{13}) = 1.000125245835038712461337524188e-7$ $T_2 = (10000^*3-20+\Delta I)/c = 1.0001252391652059378296130731621e-7$ $T_{E1} = T_{11}+T_{12}+ (10000^*2)/(c+u) = 1.334222954561797762774460365287e-7$

u

(10000-20)1

/c

=

```
In Figure 16, the following results can be obtained:
10000-\Delta I_1 = \Delta I_1 (c/u)
\Delta I_1 = 1.000592157109191600317011609584
T_{11}
                               10000/(c+u)
3.3353071903639720010567053652799e-8
                            (10000+\Delta I_1)/(c-u)
              =
3.3363085754244479779386907121003e-8
                           (T_{12}*c-T_{12}*u)/(c+u)
3.3356409185855948094456343265682e-8
Or,
                           (10000+\Delta I_1)/(c+u)
T_{13}
              =
3.3356409185855948094456343265682e-8
                            SUM(T_{11},T_{12},T_{13})
1.0007256684374014788441030403947e-7
                            (10000*3+\Delta I_1)/c
1.0007256617562109981966363213717e-7
```

 $T_{F1} = 1.3342230146516363981108806807938e-7$

By looking at the results above, we can find that when u is in the direction as in Figures 14-16, there exists time difference or OPD between the superposed light rays:

```
\Delta T (L<sub>top</sub>) = 6.669832774631724451026e-16 \Delta T (L<sub>mid</sub>) = 6.681190480647466719023e-16 \Delta T (L<sub>bot</sub>) = 6.694550187817581065588e-16
```

Let us compare the 3 ΔI_1 s of the 3 pairs of light rays above (SO = 10000):

```
\Delta I_1 (L<sub>top</sub>) = 1.0023934248822067814180813542128 \Delta I_1 (L<sub>mid</sub>) = 1.000592157109191600317011609584 \Delta I_1 (L<sub>bot</sub>) = 0.99859097279497321711637758636483
```

By comparing them, we know that the ΔI_1 s decreases from top to bottom gradually. The rough front section of all light rays when they respectively arrive at G_1 is as the red line in Figure 17.

Let us compare the 3 T_{E1} s of the 3 light rays (reflected by M_2) above (SO = 10000):

```
T_{E1} (L_{top}) = 1.334222954561797762774460365287e-7 T_{E1} (L_{mid}) = 1.3342230146516363981108806807938e-7 T_{E1} (L_{bot}) = 1.3342230814106404298426728131503e-7
```

We can find that the light rays (reflected by M_2) to the right arrive at E first. In fact, in Figure 17, we find that the light rays (reflected by M_2) to the right travel a shorter distance than that to the left. Similarly, the light rays (reflected by M_1) to the right arrive at E first.

If u is in the opposite direction, (Figure 18), the following results can be obtained:

```
10000 + \Delta I_1 = \Delta I_1 (c/u)
```

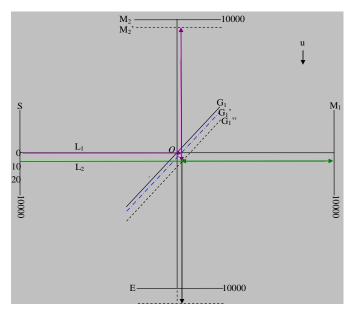


Figure 18. When u is in opposite direction.

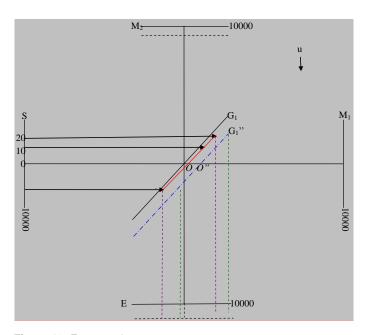


Figure 19. Front section.

$\Delta I_1 = 1.0007924341212867956934086789481$

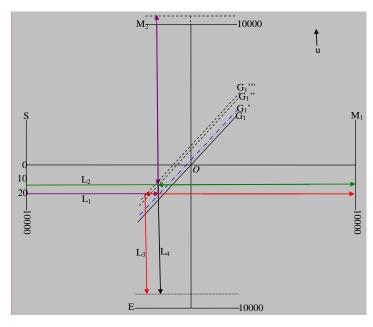


Figure 20. Reflected and transmitted lights.

$$T_2$$
 = $(10000*3-\Delta I_1)/c$ = $1.000658902752179266404503964917e-7$ $T_2 - T_1 = 6.67985345126167408452e-16$

The results show that there exists time difference or OPD between the superposed light rays.

The final result show that on view-screen light intensity to the right is higher than that to the left, except that the light rays to the left arrive at E first, as shown in Figure 19.

Looking at the following and as for transmitted light ray of L_1 :

The result shows that the reflected light ray and transmitted light ray of L_1 will arrive at E at the same time, as shown in Figure 20, where L_3 is reflected at G_1 " position, rather than at G_1 " position.

In addition, if SO is shorter, ΔI_1 is shorter accordingly (Figure 21). There is almost no OPD between the superposed light rays when u is in the directions marked in green as seen in Figure 21; and there exists OPD

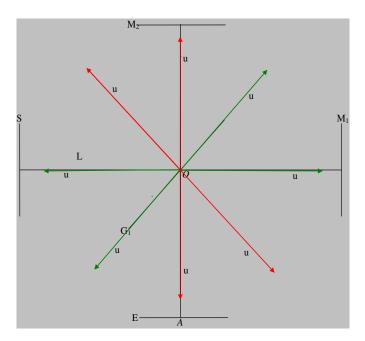


Figure 21. Overview.

between the superposed light rays when u is in the directions marked in red.

Conclusion

Through the simple, rough and surface calculations, analyses and discussion, we can generally understand that predecessors' analyses and inferences may not be satisfying in some aspects. However, the analyses above cannot perfectly explain the phenomenon: a shift of about 0.01 fringes was observed as the experimental apparatus is rotated through 90°.

To demonstrate why only a shift of about 0.01 fringes was observed, it is very possible that more complex mathematical and optical calculations and analyses need to be performed further.

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