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An overview of pore pressure prediction using seismically–derived velocities

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Knowledge of formation pore pressure ahead of the drill bit is not only critical for safe and cost-effective drilling of wells but also essential in studying the hydrocarbon trap seal and analyzing the trap configurations. A predrill estimate of the formation pore pressure can be obtained from seismic velocities and employing a velocity-to-effective stress transform. However, limitations abound in the use of seismic velocities for accurate pore pressure prediction. These limitations are traceable to some main factors such as the correctness of the seismic velocities themselves and the accuracy of the local parameters of the pore pressure prediction method used. Knowledge of the sources of overpressure in the formation is also an essential factor. This paper discusses these factors and attempts to put them into context for accurate pore pressure prediction using seismically-derived velocities.

Key words: Pore pressure prediction, overpressure, geopressure, seismic velocities, tomographic inversion, seismic inversion.

INTRODUCTION

Knowledge of the formation of pore pressure before the drill bit has become even more critical as exploration and production (E and P) of oil and gas advance into more precarious environments. In the exploration stage, knowledge of the pore pressure will ensure better assessment of the trap integrity and basin geometry, as well as hydrocarbon migration pathways. In the drilling stage, accurate pore pressure prediction is important for safe and economic drilling. Accurate pore pressure prediction is also essential for optimized casing program designed in order to avoid well control problems such as well kicks and blowouts, wellbore stability problems, stuck pipes, etc. Discussion on the subject of pore pressure has been receiving a great deal of attention for the last decades, especially in deepwater environments. Besides drilling a well, seismic survey is the only way to predict a potential geohazard subsurface zone *api-ori*. Pioneering examples in the use of seismic data for geopressure prediction include the works of Hottman and Johnson (1965), Pennebaker (1968), Reynolds (1968), Reynolds (1970, 1973).

Over the years, literature has been populated with works on the use of seismic data for predrill geopressure prediction. Of the various possible methods, the effective
stress method has become the preferred standard widely used in the industry, with the most popular method being the Eaton method (Eaton, 1975) and the Bowers method (Bowers, 1995). Even with the sophistication of parameters now in use and the range of software now available, limitations still abound in the use of seismic data for accurate pore pressure prediction. These limitations can be traceable to the following main factors:

1. Poor knowledge of the various sources of overpressure in the formation.
2. The problem of accurate determination of the local parameters of the pore pressure prediction method used.
3. Correctness of the seismic velocities themselves and the quality of the seismic data acquisition and processing technology.

This paper discusses these factors and highlights how they can be conditioned to ensure accurate pore pressure prediction using seismically-derived velocities.

**SOURCES OF OVERPRESSURE**

The processes which generate overpressure in Tertiary basins where deposition and subsidence occur very rapidly can be categorized into three groups. The ability of each group to generate overpressure depends on the rock and fluid properties and their rate of change with the varying basin conditions.

**Mechanisms related to increase in stress:**

The primary source of overpressure in Tertiary basins is believed to be mechanical compaction disequilibrium in low permeability sediments. If the low permeability sediment does not allow the escape of the confined pore fluid at rates sufficient to keep with the rate of increase in vertical stress, in order to maintain a hydrostatic pressure gradient, the pore fluid is forced to carry a large part of the combined weight of the overlying rocks and fluids. This leads to increase in pore fluid pressure and results in under compaction or compaction disequilibrium in the rapidly accumulating sediment. This type of overpressure mechanisms is observed mainly in young tertiary basins worldwide and is commonly recognized in seismic velocity data by the slow decrease in velocity with depth.

Overpressure due to compaction disequilibrium at a given depth is usually depicted by increase in porosity and typically occurs where there is a sand-rich to shale-rich environment. On pressure–depth plot (Figure 1), the mechanism is characterized by a fluid retention depth (FRD) at which overpressure starts and increases downwards along a gradient parallel to the lithostatic pressure gradient. This results in a constant vertical effective stress below the fluid retention depth and hence no further mechanical compaction or reduction in porosity takes place.

Another source of overpressure related to increase in stress is that related to tectonism (lateral compressive stress). This process is similar to undercompaction in that the increased vertical stress is taken up by the trapped pore fluid leading to an overall increase in geopressure (Dutta, 1987). However, unlike undercompaction, tectonic loading is capable of generating high overpressure (Bowers, 2002).

**Mechanisms related to fluid volume expansion**

A host of other overpressure generating mechanisms
occur in addition to the primary undercompaction or compaction disequilibrium sources leading to the pore fluid volume expansion. These secondary mechanisms are usually due to in-situ fluid generating mechanisms which cause the pore pressure to increase at a fixed overburden, resulting in decrease of the effective stress on the matrix (Chopra and Huffman, 2006). Hence they are also known as unloading mechanisms. Some of the major mechanisms related to fluid volume expansion (Swarbrick and Osborne, 1998) include: aquathermal expansion, hydrocarbon source generation/maturation, clay diagenesis and oil to gas cracking.

Although the processes of overpressure generation in these mechanisms are distinctly different in their behaviour, they all produce similar effect in the rocks by resulting in the fluid volume expansion and the unloading mechanism of the formation for a given porosity. These overpressure mechanisms are commonly depicted by the reversal in the velocity trend with depth without an increase in porosity. Although not all velocity reversals are caused by overpressure, it is reasonable to treat velocity reversal as diagnostic feature of overpressure unless there is sufficient evidence from the well data to conclude that the velocity reversals are otherwise due to undercompaction, change in lithology or other possible causes. A deterministic indicator of high overpressure is when the sonic velocity and resistivity data have larger reversals than the bulk density data. This follows because transport properties such as sonic velocity, permeability and resistivity generally undergo more elastic rebound than bulk density and porosity (Bowers and Katsube, 2002).

**Mechanisms related to fluid movement and buoyancy**

These include other minor overpressure generating sources such as osmosis, hydrocarbon buoyancy, lateral transfer and hydraulic head (Swarbrick and Osborne, 1998). Figure 2 shows the pressure trend and response of vertical effective stress (VES) to different overpressure generating mechanisms.

**PORE PRESSURE PREDICTION METHODS**

Most methods of pore pressure predictions are based on Terzaghi’s effective stress relation (Terzaghi, 1943) that expresses elastic wave velocity as a function of vertical effective stress. Since the stress is normal, it can otherwise be called pressure and be used interchangeably. The effective pressure, \( \sigma \), is the
pressure acting on the solid rock matrix. It is defined as the difference between the overburden pressure, $S$, and the pore pressure, $P$. Terzaghi's relation extended to solid rocks can be written as:

$$\sigma = S - \alpha P$$  \hfill (1)

Where $\alpha$ is the poro-elastic coefficient, and is the ratio of the effect of fluid pressure on VES with the effect of overburden stress on VES. The poro-elastic coefficient is introduced in Terzaghi's original equation when applied to consolidated rocks to take care of the effect of decrease in fluid pressure now applied on less of the grain surface. Generally, $\alpha < 1$ and has a value between 0.7 and 1.0; for over pressured rocks, $\alpha$ is usually around 0.8.

The overburden pressure is the pressure due to the combined weight of the rock matrix and the fluids in the pore space overlying the formation of interest at a given depth. The overburden pressure $S$ can be expressed as integral of density:

$$S = g \int_0^z \rho(z) \, dz$$  \hfill (2)

Where $\rho(z)$ is the bulk density of the formation as a function of depth, $z$, and $g$ is the acceleration due to gravity. The bulk density can be obtained from a density log, if available. In the absence of the shallow density log, the sediment density, $\rho_s$, can be estimated using the density correlation (Zhang et al., 2008):

$$\rho_s = \phi \rho_w + \rho_m (1 - \phi)$$  \hfill (3)

Where $\phi$ is fractional porosity, $\rho_w$ is the density of the pore water (1.03g/cm$^3$) and $\rho_m$ is the average density of the sediment matrix. Alternatively, the sediment density can also be estimated from seismic velocity using the empirical relation of Gardner et al. (1974):

$$\rho_s = a V^b$$  \hfill (4)

Where $V$ is the seismic interval velocity, $a$ and $b$ are lithology–dependent parameters.

The compaction process of sedimentary rocks is essentially controlled by the effective stress. Hence any condition at a given depth that brings about a decrease in effective stress will ultimately lead to a decrease in the compaction rate (higher porosity) and consequently result in overpressure. Low effective stress and high porosity tend to lower the rock velocity. Thus, in young Tertiary basins such as the Niger, Nile and Mississippi deltas, Gulf of Mexico and Baran basins with thick intervals of shale and high sedimentation rate, it is geologically reasonable to use velocity as proxy for porosity retention to predict overpressure. Relationships between the rock velocity and the effective stress, and pore pressure, abound in literature (Hottman and Johnson, 1965; Mathew and Kelly, 1967; Eaton, 1972, 1975; Bowers, 1995; 2001; Flemmings et al., 2002).

If the relation between elastic wave velocity and vertical effective stress is known, the pore pressure $P$ can be calculated from Equation 1, and the total overburden stress determined from Equation 2. Most common methods used for determining pore pressure from compressional seismic velocity include the Eaton’s method, Bowers’ method and the Tau model. The choice for each method depends on the overpressure generation mechanism in the area of interest.

**Eaton’s method**

Eaton (1975) in accordance with Terzaghi (1943) presented an empirical relation for the pressure from compression transit time:

$$P = S - (S - P_{hyd}) \left(\frac{\Delta t_n}{\Delta t}\right)^3$$  \hfill (5)

Where $P$ is the formation pressure, $S$ is the overburden pressure, $P_{hyd}$ is the hydrostatic pressure, $\Delta t$ is the transit time in shales obtained from seismic data and $\Delta t_n$ is the transit time in shales at normal compacted pressure.

Eaton’s method applies predominantly to thick shale-rich lithology where overpressure is primarily due to disequilibrium compaction. Although Eaton’s method is applicable in some petroleum basins, it has some limitations because it does not consider unloading effects. This implies that the method is valid only when the normal compaction trend can be constructed for all depths of interest. Hence the model cannot be applied in geologically complicated areas, such as formations with uplifts or high sedimentation rates, as is common in deepwater environment.

Considering the limitations of the original Eaton’s method, Bowers (1995) proposed a modified Eaton’s method of the form:

$$P = S - (S - P_{hyd}) \left(\frac{\Delta t_n}{\Delta t}\right)^n$$  \hfill (6)

Where the exponent $n$ describes the sensitivity of velocity to differential stress. The value of $n$ depends on the geological formation being investigated ($n>3$). When the exponent in Equation 6 becomes greater than 3, the model can simulate the unloading curves.

**Bowers’ method**

Bowers (1995) proposed that the compressional velocity,
Vertical effective stress (kpsi) vs. Velocity (ft/s)

**Figure 3.** Shale compaction/elastic rebound (Bowers, 2001).

\[
V_p = V_{ml} + A\sigma^B \tag{7}
\]

Where \( V_{ml} \) is the compressional velocity at the mudline (usually 5000 ft/s), \( A \) and \( B \) are the parameters calibrated with offset velocity versus effective stress data.

The loading curve of \( V_p \)-VES plot of Equation 8 is however, not obeyed when there is unloading or formation uplift. A higher than the velocity in the loading curve occurs at the same effective stress. Bowers (1995) proposed an empirical relation to account for the unloading effect:

\[
V_p = V_{ml} + A\left[\frac{\sigma}{\sigma_{max}}\right]^{1/2} \tag{8}
\]

Where \( U \) is the unloading parameter and is a measure of how plastic the sediment is. \( U \) is calibrated with local data and practically ranges from 3-8 in unloading cases. \( \sigma_{max} \) is the maximum effective stress at the beginning of the unloading and depicted by a rebound on the Vp-VES cross-plot.

Note that when \( \sigma = \sigma_{max} \), then \( V_p = V_{max} \).

Hence \( \sigma_{max} \) can be expressed as:

\[
\sigma_{max} = \left[\frac{1}{A}(V_{max} - V_{ml})\right]^{1/2} \tag{9}
\]

It then follows that \( \sigma_{max} \) and \( V_{max} \) are respectively the estimates of the effective stress and velocity at the onset of unloading. Note also, that if the unloading exponent \( U \) in Equation 8 equals unity, then the stress ratio term in the expanded equation returns to the same form of equation for the normal compaction trend/loading curve. The unloading curve has a flatter effective stress path than the initial/virgin curve (Figure 3).

**Tau Model**

The Tau variable was introduced into the effective stress equation in a transit time dependent pore pressure prediction method (Lopez et al., 2004; Zhang and Wieseneck, 2011). This is an empirical relationship linking velocity to vertical effective stress:

\[
\sigma = A\tau^B \tag{10}
\]

Where \( A \) and \( B \) are fitting constants derived from local data and the Tau variable \( \tau \), is the scaled sonic which can be defined as:

\[
\tau = \frac{C-\Delta t}{\Delta t-D} \tag{11}
\]

Where \( \Delta t \) is the transit time from either sonic log or seismic velocity, \( C \) and \( D \) are constants related to the mudline and matrix transit time respectively.

The pore pressure calculation of Terzaghi (1943), using the Tau model then becomes

\[
P = S + A\left[\frac{C-\Delta t}{\Delta t-D}\right]^B \tag{12}
\]

The power law nature of Equation 10 is theoretically sound and in practice has been widely proven to give...
more robust and excellent fit (Opara et al., 2013). It should be noted that the pore pressure prediction methods described in this paper are all based on the rock properties in shales. Hence the pore pressures obtained from these methods are the pressures in shales. For the pressures in sand, sandstones or other permeable formations, the formation pore pressure can be obtained by assuming that the shale pressure is equal to the sandstone pressure or using fluid flow model (Traugott, 1997; Zhang, 2011) to calculate the pressure.

### SEISMIC VELOCITIES FOR PORE PRESSURE PREDICTION

The accuracy of predrill pore pressure prediction largely depends on the type of seismic velocity used for the velocity-pressure transformation and the quality of the data conditioning. Many types of seismic velocity analysis exist but for well planning purposes, the seismic velocities should be derived using methods that give sufficient spatial resolutions.

In the presence of complex or steeply dipping structures, the resolutions obtained from the conventional stacking velocity analysis are usually too low for accurate pore pressure prediction due to the layered earth model and hyperbolic move out assumptions. High resolution velocity analyses that have been used with varying degrees of success include the horizon-keyed velocity analysis, reflection tomography and seismic inversions. These techniques yield more robust geopressure predictions, though at higher cost. The resolution and accuracy of each technique depends, to a large extent, on the geologic scenario that plays out and on the expertise of the pressure interpreter.

#### Horizon – keyed velocity analysis

The horizon–keyed velocity analysis (HVA) provides accurate velocities at every CMP location along selected key horizons, as opposed to the conventional velocity analysis that is usually carried out at selected CMP locations. HVA is usually carried out using a small number of time gates centered on normal incidence travel times that track the given reflection horizons. The technique has been proven to be an efficient velocity analysis for geopressure prediction (Yilmaz, 1987).

#### Reflection tomography

In contrast to interval velocities resulting from conventional velocity analysis, reflection tomography (Stork, 1992; Woodward et al., 1998; Bishop et al., 1985), provides more detailed interval velocities necessary for predrill pore pressure prediction in terms of the spatial resolution. The velocity field resulting from reflection tomography better relates to the 3D geologic structures than that realizable with conventional stacking velocity analysis.

Reflection tomography is basically a 3D traveltime inversion process. The input to the process consists of travel time picks of the seismic reflection events and a first-guess velocity of the subsurface structure which characterizes the model. This is usually done in the depth domain rather than the time domain. Following the picking of the travel times from the seismic data and the computation of the travel times by ray tracing (Aki and Richards, 1980), the difference (misfit) between the two travel times is used to solve the least-squares equation of the form:

\[ \Delta T = D \Delta S \]  

Where \( \Delta T \) is the difference between the real travel time picked from the seismic data and that estimated by ray tracing through the model. \( D \) is an nxm matrix containing the ray distances, \( n \) is the number of ray paths and \( m \) is the number of slowness cells.

The least–squares slowness solution obtained is used to refine and update the original slowness model. The process is iterated until variations in \( \Delta S \) become insignificantly small. When properly conditioned, the tomography inversion velocity can provide a reliable velocity field which can closely relate to the rock velocity of the subsurface structure. Figure 4 shows the PSDM seismic sections from the Gulf of Mexico obtained by Woodward et al. (1998) using velocities derived by
Figure 5. Pore pressure predictions (ppg) obtained using conventional stacking velocity (a) and tomographic velocity (b) (Sayers et al., 2002).

conventional stacking velocity (a) and velocity field refined by reflection tomography (b). Significant improvement in the seismic image is obtained with the velocity field refined by reflection tomography compared to that obtained by conventional stacking velocity field.

Sayers et al. (2002) demonstrates the pore pressure predictions arising from the two velocity fields (Figure 5). Although the velocity obtained from the stacking velocity analysis predicts the presence of overpressure in this area, the pore pressure prediction from the tomographically refined velocity model is more dramatic in terms of the magnitude and spatial resolution. Thus, robust pore pressure prediction requires very accurate velocity field with high spatial resolution akin to the tomographically refined velocity model.

Seismic inversion velocities

Seismic inversion generally refers to transformation of seismic amplitudes (prestack or postack) into acoustic impedance values. It is an integration of data from several sources, seismic, well log and/or velocity. Hence a good quality impedance model contains more information than the seismic reflection data. Acoustic impedance (product of velocity and rock density) being a layer property, and not an interface property, allows direct interpretation of 3D geologic structures.

For pore pressure prediction, seismic inversion can be carried out as a means of refining the velocity field in order to improve the resolution, and as a means of removing unwanted data from the pressure calculation. Usually, the inversion technique begins with a reliable velocity field. The velocity field is then refined and updated by the process.

Prestack inversion

Prestack seismic amplitude inversion methodologies are wave-equation–based. These full waveform techniques represent the generalized multidimensional inversion that allows the estimation of density and velocities ($V_s$ and $V_p$) simultaneously, using the near offset reflectivity and amplitude versus offset behavior of each reflection event in the subsurface. This allows the user to estimate the overburden and effective stress from the same data set. They generally use seismic gathers as seed to produce the velocity model. The method employs inversion schemes based on nonlinear least–squares and updates the earth parameters iteratively in order to monotonically minimize the misfit between the observed and the modeled data.

Mallick (1999) developed a generic algorithm (GA) for prestack inversion which can be used to obtain the $P$-wave and the $S$-wave velocity models, and densities for a given seismic gather by minimizing the mismatch between the observed angle gathers and their corresponding synthetic computations. The process is iterated until the fitness values in the synthetic models converge.

Figure 6 shows the result of the application of the generic algorithm approach by Dutta (2002) to the CMP gathers for the stacked data, and the corresponding synthetic stacks. The biggest challenges to prestack inversion in pore pressure prediction, other than cost, are its extreme sensitivity to data quality and the need to
incorporate the low-frequency velocity trend in the analysis which has its own attendant problems.

**Postack inversion**

Postack amplitude inversion like the prestack inversion provides high resolution by inverting for impedance from the seismic reflection services represented by the geologic formations. Seismic wavelet side lobes are removed from the reflection events to obtain estimates of residual impedance for each layer/lithology. The inversion can be used to generate estimates of the absolute impedance \( I_p \) and \( I_s \) or its components of velocity and density \( V_p, V_s, \rho \).

Postack inversion can be applied using only the stacked seismic data or can be calibrated with well logs, check shot or VSP data. Figure 7 shows the difference in resolution between conventional horizon–keyed velocity analysis and postack inversion presented by Huffman (2002). The postack inversion results show higher resolutions of the seismic traces.

**Conclusion**

Pore pressure prediction is key to safe and economic drilling. Pore pressure prediction from seismic survey uses seismically derived velocities to estimate the formation pore pressure. However, limitations abound in the use of seismic data for accurate pore pressure prediction, especially in precarious complex/steeply
dipping structures or deepwater environment. Although there are different methods of estimating formation pore pressure, the applicability and accuracy of each method depends on accurate determination of the local parameters of the pore pressure prediction method used, the formation geology, the correctness of the seismic velocities and quality of the seismic data acquisition and conditioning.

The pressure interpreter should have a good understanding of the overpressure sources in the formation to be able to relate the pressure trend and response of vertical effective stress to the different overpressure generating mechanisms. Pore pressure prediction using seismic data requires seismic velocities that are dense and accurate and are close to the formation velocities under consideration. Such velocities with high resolutions akin to the tomographically refined velocities and inversion velocities yield robust geopressure predictions, though at higher cost.

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