Full Length Research Paper

Comparison of improved nonlinear static procedures for spatial steel trusses supported on steel columns

Zeki AY

Department of Civil Engineering, Suleyman Demirel University, Isparta, 32260, Turkey. E-mail: zekia@mmf.sdu.edu.tr. Tel: +90-246-211-1199. Fax: +90-246-237-0859.

Accepted 6 July, 2010

The most significant expectation for ages has been building structures which are as high as possible, without column and wide-spanned in architecture. Also it is vital to cover these structures as spatial trusses. Similarly; economic, rapid, safe and aesthetical solutions in space systems are possible by spatial steel structures. In last decades, ATC 40, FEMA 273, 274, 356 and recently 440 are the most commonly used resources for seismic analysis procedures enduring with computing in civil engineering. These procedures are defined as displacement based performance analysis. On the other hand, nonlinear static procedures as basic step of these methodologies still have some problems in theoretical background. Some of the researchers are not satisfied with the accuracy of current performance based design methodologies. There are some question marks on how accurate capacity and demand spectrums demonstrate the structural capacity and earthquake demand respectively. In this study, comparison of improved nonlinear static procedures in FEMA- 440 has been made for spatial steel trusses supported on steel columns. For this, numerical models which are set up by taking structural properties of evaluable structures are investigated by using improved nonlinear static procedures which are given in FEMA- 440. Differences and harmonies of methods are still been determined.

Key words: Spatial steel structures, nonlinear seismic procedures.

INTRODUCTION

The determination of the displacement demand of structures subjected to seismic actions is one of the most important steps in performance based design procedures. In last decades, significant progress was made in performance-based engineering methods that rely on non-linear static analysis procedures (NSPs). Nonlinear static procedures are one type of inelastic analysis that can be used to estimate the response of structures to seismic actions. In practice, the current procedures can result in estimates of maximum displacement that are significantly different from one another. The differences between the various approaches relate to the level of detail of the structural model and the characterization of the seismic ground shaking. This is one of the major areas of concern of practicing engineers. Current nonlinear static procedures are Coefficient Method in FEMA-356 (Applied Technology Council, 1996) and Capacity-Spectrum Method in ATC-40 (Federal Emergency Management Agency, 2000; Applied Technology Council,

2005). The two approaches are essentially the same when it comes to generating a "pushover" curve to represent the inelastic force-deformation behavior of a building. They differ, however, in the technique used to calculate the inelastic displacement demand for a given representation of ground motion. Various researchers and practicing engineers have found that in some cases, different inelastic analysis methods give substantially different estimates for displacement demand for the same ground motion and same SDOF oscillator or same building (Chopra and Goel, 2002, 2004, 1999; Chopra et al., 2004; Goel and Chopra, 2004; Aydinoglu, 2003). Recently, a new document was published about nonlinear static procedures. This document has proposed two new procedures instead of Capacity-Spectrum Method of ATC- 40 and Coefficient Method of FEMA-356 (Applied Technology Council, 1996). These new procedures are Displacement Modification and Equivalent Linearization methods (Applied Technology Council, 2005; UBC, 1997). The Capacity-Spectrum Method and Displacement Coefficient Method rely on different underlying relationships to estimate the response of nonlinear systems based on an elastic response spectrum. The Capacity-Spectrum Method relies on the concept of equivalent linearization while the Displacement Coefficient Method uses $R-\mu-T$ relationships. As presented and utilized currently; the graphical characteristics of the two procedures are also different.

However, these differences are not fundamental and results from either approach may be readily transformed into various graphical representations (Kalkan and Kunnath, 2007; Chintanapakdee and Chopra, 2003; Gupta and Kunnath, 2000; Kunnath and Kalkan, 2004; Bozorgina and Bertero, 2004 Fajfar and EERI, 2000 Naeim, 2003; Makowski, 1988). The peak displacement of a nonlinear system is estimated as the intersection of the capacity curve and an elastic response spectrum that is reduced to account for energy dissipated by the vielding structure. The underlying basis of the Capacity-Spectrum Method (CSM) is the concept of an "equivalent linear" system, wherein a linear system having reduced stiffness and increased damping proportional to hysteretic energy, is used to estimate the response of the nonlinear system. The CSM is documented thoroughly in ATC-40 (Applied Technology Council, 1996; Federal Emergency Management Agency, 2000; Applied Technology Council, 2005).

In wide-span structures, spatial steel trusses are preferred instead of classical steel roof constructions. They provide economic solutions in using the wide gaps in diverse geometries passing without columns as indoors. Spatial steel trusses are used in places such as industrial areas, factories, air-plane and helicopter hangars, swimming-pools, sport-centers, storerooms, theateropera saloons, cinemas, stands, shop, school buildings, laboratories and fair-departments and in addition, they are highly economic structures (Ay, 1994; Dikmen and Ay, 2006; Korkmaz et al., 2008; Ay and Durmuş, 2002; Fenkli and Ay, 2004: 24).

On the other hand, some of the researchers are not satisfied with the accuracy of current performance based design methodologies. Therefore, current nonlinear static procedures as basic step of these methodologies still have some problems in theoretical background. In other words, there are some question marks on how accurate capacity and demand spectrums demonstrate the structural capacity and earthquake demand, respectively. For this reason, it is very important that comparison of improved nonlinear static procedures in FEMA- 440 for spatial steel trusses supports the steel columns.

Definition of structural models

Steel spatial frames on the steel columns are used as closed

market area. Different than the residential buildings, snow, wind, and other roof weights are distributed to the foundations through columns. Lateral stability is responded by the columns in such onestory longer spanned spatial systems. Therefore, geometrical properties of roof and columns play an important role in structural behavior.

In the present study, 4 different soil classes were considered. Shear velocities for the soil classes are; 1000, 600, 300 and 150 m/sn for B, C, D, and E soil classes, respectively. Embedment e = 0 and damping is not considered for each model. Design earthquake is selected as an earthquake with exceeded probability of 10% in 50 years. Mapped short-period spectral response Acceleration Ss =1, for 1 s period, Mapped Spectral Response Acceleration at one-second period S1 = 0.4 for 1st earthquake zone and 0.3 for 2nd zone, 0.2 for 3rd zone and 0.1 for 4th zone. Hence, according to Turkish earthquake code (TEC), 4 different earthquake zones and 4 soil classes and 3 different structural models (Figure 1), nonlinear static procedure, were used according to FEMA 440 (Applied Technology Council, 2005). Table 1 presents seismic coefficients according to TEC'07 and UBC'97 (UBC, 1997; Turkish Earthquake Code, 2007).

The selected models in the study were; broken, flat model and vault. The area of the broken model is 48×48 m, weight is 1940 kN. The area of flat model is 66×53 m and the weight is 750kN. The area of Vault model is 32*48 m and the weight is 410 kN. Minimum column height is 5 m, column sections are HE400A. For steel roof, different types of steel sections were used. Used steel is A36. Earthquake loads were applied for only X direction.

RESULTS

Comparison of base shear, displacements and spectral acceleration graphs for broken model are given in Figures 2, 3 and 4, respectively. Same comparison for flat model can be seen in Figures 5, 6 and 7, respectively. Finally, Figures 8, 9 and 10 display vault model comparison. Tables 2 and 3 showed comparison results for Broken model for X and Y direction, respectively. In Tables 4 and 5, comparison of improved nonlinear static procedures for flat model can be seen for X and Y direction, respectively. Same comparison is given in Tables 6 and 7 for Vault model for X and Y direction, respectively.

CONCLUSION

In this paper, improved nonlinear static procedures according to FEMA 440 are compared for spatial steel trusses placed on steel columns. In the analysis of three structural models, SAP 2000 computer program was performed (Computer and Structures Inc., 2004). Performance points of models Displacement, acceleration, and base shear force were found by using Displacement Modification and Equivalent Linearization methods. Following conclusions were delineated as a result of numerical analysis:

1. In terms of base shear values, in the broken model,



Figure 1. Structural models.

| Table 1. | Seismic Coefficients | C_a , C_v | v (TEC 2007 - UBC 97) TEC: Turkish Earthquake Code 2007. |
|----------|----------------------|---------------|--|
|----------|----------------------|---------------|--|

| Site class | UBC: ** TEC: 4 A₀=0,10 n=0.80 | | UBC : 2B TEC: 3 A ₀ =0,20 n=0.70 | | UBC: 3 TEC: 2 A₀=0,30 n=0.65 | | UBC : 4 TEC: 1 A₀=0,40 n=0.60 | |
|----------------------------------|--|------|--|------|---------------------------------------|------|--|--------------------|
| | Ca | Cv | Ca | Cv | Ca | Cv | Ca | Cv |
| S _B (Z ₁) | 0.10 | 0.10 | 0.20 | 0.20 | 0.30 | 0.30 | 0.40N _a | $0.40N_v$ |
| S _C (Z ₂) | 0.12 | 0.17 | 0.24 | 0.32 | 0.33 | 0.45 | 0.40Na | 0.56Nv |
| S _D (Z ₃) | 0.15 | 0.23 | 0.28 | 0.40 | 0.36 | 0.54 | $0.44N_a$ | $0.64N_{v}$ |
| S _E (Z ₄) | 0.23 | 0.34 | 0.34 | 0.64 | 0.36 | 0.84 | 0.36N _a | 0.96N _v |

A_{0 =} Effective Ground Acceleration Coefficient, n: Aproximate values of shear wave velocity reduction factor. Na and Nv:



Figure 2. Comparison of base shear for broken model. (a) X direction, (b) Y Direction.







Figure 4. Comparison of spectral acceleration for broken model direction. (a) X direction,(b) Y direction.



Figure 5. Comparison of base shear for flat model. (a) X direction, (b) Y direction.



Figure 6. Comparison of Displacement for Flat Model Y a ,b Direction



Figure 7. Comparison of Spectral Acceleration for Flat Model



Figure 8. Comparison of base shear for vault model. (a) X direction, (b) Y direction.



Figure 9. Comparison of Displacement for Vault Model



Figure 10. Comparison of Spectral Acceleration for Vault Model

| Seismic | Site | Equiva | alent lineari | zation | Displacement modification | | | |
|---------|-------|---------|---------------|--------|---------------------------|---------------------|-------|--|
| zone | class | V (kN) | D (mm) | Sa | V _y (kN) | D _y (mm) | Sa | |
| | Z1 | 1450.68 | 45.84 | 0.848 | 1397.95 | 43.95 | 0.795 | |
| D1 | Z2 | 1732.98 | 56.45 | 0.918 | 1610.75 | 51.85 | 0.923 | |
| | Z3 | 1837.64 | 63.26 | 0.975 | 1763.91 | 58.12 | 1.015 | |
| | Z4 | 1534.91 | 49.01 | 0.869 | 1462.69 | 46.29 | 0.830 | |
| | | | | | | | | |
| | Z1 | 1088.62 | 33.91 | 0.646 | 1037.38 | 32.53 | 0.595 | |
| DO | Z2 | 1390.96 | 43.72 | 0.825 | 1341.09 | 42.10 | 0.761 | |
| DZ | Z3 | 1534.91 | 49.01 | 0.869 | 1462.69 | 46.29 | 0.830 | |
| | Z4 | 1534.91 | 49.01 | 0.869 | 1462.69 | 46.29 | 0.831 | |
| | | | | | | | | |
| | Z1 | 725.75 | 22.13 | 0.430 | 336.21 | 10.54 | 0.199 | |
| Da | Z2 | 1011.58 | 31.41 | 0.600 | 572.33 | 17.95 | 0.338 | |
| D3 | Z3 | 1180.18 | 36.88 | 0.700 | 812.11 | 25.46 | 0.477 | |
| | Z4 | 1436.13 | 45.29 | 0.845 | 1219.53 | 38.24 | 0.695 | |
| | | | | | | | | |
| | Z1 | 362.87 | 10.35 | 0.215 | 336.21 | 10.54 | 0.199 | |
| D4 | Z2 | 505.79 | 14.99 | 0.300 | 466.66 | 14.63 | 0.277 | |
| D4 | Z3 | 632.24 | 19.10 | 0.375 | 620.01 | 19.44 | 0.369 | |
| | Z4 | 969.43 | 30.04 | 0.575 | 995.84 | 31.22 | 0.577 | |

 Table 2. Broken (X) comparison of improved nonlinear static procedures (FEMA 440).

Table 3. Broken (Y) Comparison of Improved Nonlinear Static Procedures (FEMA 440).

| Seismic | Site | Equivalent linearization Displacement mod | | | | | ification |
|------------|-------|---|--------|-------|---------------------|---------------------|-----------|
| zone | class | V (kN) | D (mm) | Sa | V _y (kN) | D _y (mm) | Sa |
| | Z1 | 1027.67 | 68.06 | 0.589 | 1013.91 | 65.55 | 0.595 |
| | Z2 | 1173.48 | 94.59 | 0.671 | 1164.62 | 92.98 | 0.833 |
| D1 | Z3 | 1245.53 | 107.71 | 0.712 | 1249.77 | 108.48 | 0.952 |
| | Z4 | 1238.32 | 106.39 | 0.708 | 1183.32 | 96.39 | 0.852 |
| | Z1 | 822.67 | 51.36 | 0.471 | 774.39 | 48.36 | 0.446 |
| Da | Z2 | 1073.48 | 76.40 | 0.615 | 1060.77 | 74.08 | 0.670 |
| D2 | Z3 | 1155.38 | 91.30 | 0.661 | 1148.73 | 90.09 | 0.804 |
| | Z4 | 1238.32 | 106.39 | 0.708 | 1183.33 | 96.39 | 0.852 |
| | Z1 | 548.44 | 34.21 | 0.314 | 243.61 | 15.21 | 0.149 |
| D 2 | Z2 | 877.51 | 54.79 | 0.503 | 419.92 | 26.23 | 0.253 |
| D3 | Z3 | 1027.67 | 68.06 | 0.589 | 602.48 | 37.63 | 0.357 |
| | Z4 | 1198.46 | 99.14 | 0.685 | 915.68 | 57.19 | 0.521 |
| D4 | Z1 | 274.22 | 17.06 | 0.157 | 243.61 | 15.21 | 0.149 |
| | Z2 | 466.18 | 29.06 | 0.267 | 419.92 | 26.23 | 0.253 |
| | Z3 | 630.71 | 39.36 | 0.361 | 602.48 | 37.63 | 0.357 |
| | Z4 | 932.35 | 58.23 | 0.534 | 915.68 | 57.19 | 0.521 |

results of each method are close to each other. For theother models, a significant difference is observed. This

shows that structural geometry is one of the important parameters.

| Seismic | Site | Equivalent linearization Displacement modification | | | | | fication |
|---------|-------|--|-------|-------|----------------------|---------------------|----------|
| zone | class | V(kN) | D(mm) | Sa | V _{y(} (kN) | D _y (mm) | Sa |
| | Z1 | 866.26 | 3.65 | 1.00 | 576.14 | 2.25 | 0.788 |
| | Z2 | 866.26 | 3.65 | 1.00 | 523.37 | 2.04 | 0.788 |
| D1 | Z3 | 951.36 | 3.98 | 1.098 | 480.05 | 1.87 | 0.865 |
| | Z4 | 566.32 | 2.50 | 0.654 | 278.51 | 1.09 | 0.515 |
| | | | | | | | |
| | Z1 | 649.70 | 2.82 | 0.750 | 430.32 | 1.68 | 0.591 |
| 50 | Z2 | 714.67 | 3.07 | 0.825 | 429.57 | 1.68 | 0.650 |
| DZ | Z3 | 764.25 | 3.26 | 0.882 | 380.88 | 1.49 | 0.695 |
| | Z4 | 602.68 | 2.64 | 0.696 | 297.11 | 1.16 | 0.548 |
| | | | | | | | |
| | Z1 | 433.13 | 1.98 | 0.500 | 285.70 | 1.12 | 0.394 |
| Da | Z2 | 519.76 | 2.32 | 0.600 | 310.35 | 1.21 | 0.472 |
| D3 | Z3 | 606.38 | 2.65 | 0.700 | 299.02 | 1.17 | 0.552 |
| | Z4 | 635.00 | 2.76 | 0.733 | 366.28 | 1.43 | 0.670 |
| | | | | | | | |
| D4 | Z1 | 216.57 | 1.14 | 0.250 | 142.26 | 0.56 | 0.197 |
| | Z2 | 259.88 | 1.31 | 0.300 | 153.80 | 0.60 | 0.236 |
| D4 | Z3 | 314.34 | 1.52 | 0.363 | 164.48 | 0.64 | 0.309 |
| | Z4 | 492.52 | 2.21 | 0.569 | 265.81 | 1.04 | 0.492 |

Table 4. Flat (X) comparison of improved nonlinear static procedures (FEMA 440).

Table 5. Flat (Y) comparison of improved nonlinear static procedures (FEMA 440).

| Seismic | Site | Equiv | alent lineariz | zation | Displacement modification | | | |
|---------|-------|--------|----------------|--------|---------------------------|---------------------|-------|--|
| zone | class | V(kN) | D(mm) | Sa | V _{y(} (kN) | D _y (mm) | Sa | |
| | Z1 | 866.26 | 7.63 | 1.00 | 584.82 | 4.93 | 0.788 | |
| | Z2 | 866.26 | 7.63 | 1.00 | 538.88 | 4.54 | 0.788 | |
| D1 | Z3 | 952.89 | 8.35 | 1.10 | 513.52 | 4.33 | 0.866 | |
| | Z4 | 685.03 | 6.12 | 0.791 | 356.10 | 3.00 | 0.623 | |
| | Z1 | 649.70 | 5.83 | 0.75 | 434.73 | 3.66 | 0.591 | |
| 50 | Z2 | 714.67 | 6.37 | 0.825 | 439.80 | 3.71 | 0.650 | |
| DZ | Z3 | 779.64 | 6.91 | 0.900 | 410.53 | 3.46 | 0.709 | |
| | Z4 | 738.34 | 6.56 | 0.852 | 386.62 | 3.26 | 0.672 | |
| | Z1 | 433.13 | 4.03 | 0.500 | 287.26 | 2.42 | 0.394 | |
| 20 | Z2 | 519.76 | 4.75 | 0.600 | 315.41 | 2.66 | 0.472 | |
| 03 | Z3 | 606.38 | 5.47 | 0.700 | 311.82 | 2.63 | 0.552 | |
| | Z4 | 736.32 | 6.55 | 0.850 | 385.46 | 3.25 | 0.670 | |
| | Z1 | 216.57 | 2.23 | 0.250 | 142.36 | 1.2 | 0.197 | |
| D4 | Z2 | 259.88 | 2.59 | 0.300 | 154.75 | 1.30 | 0.236 | |
| D4 | Z3 | 324.85 | 3.13 | 0.375 | 171.77 | 1.45 | 0.315 | |
| | Z4 | 498.10 | 4.57 | 0.575 | 275.91 | 2.32 | 0.493 | |

2. For Broken model, base shear, displacement and acceleration values were in harmony. However, in the

other axis (Y axis), especially for the 3rd earthquake zone, this harmony dissolves. This shows that earthquake zone

| Seismic | Site | Equiva | alent lineariz | zation | Displacement modification | | | |
|---------|-------|--------|----------------|--------|---------------------------|---------------------|-------|--|
| zone | class | V(kN) | D(mm) | Sa | V _{y(} (kN) | D _y (mm) | Sa | |
| | Z1 | 331.84 | 3.37 | 1.00 | 196.72 | 1.91 | 0.788 | |
| | Z2 | 322.22 | 3.28 | 0.971 | 172.96 | 1.68 | 0.765 | |
| D1 | Z3 | 346.62 | 3.52 | 1.045 | 154.31 | 1.49 | 0.823 | |
| | Z4 | 208.99 | 2.19 | 0.630 | 90.90 | 0.88 | 0.496 | |
| | | | | | | | | |
| | Z1 | 248.88 | 2.57 | 0.750 | 146.76 | 1.42 | 0.591 | |
| 20 | Z2 | 269.99 | 2.78 | 0.814 | 144.20 | 1.39 | 0.641 | |
| DZ | Z3 | 278.63 | 2.86 | 0.840 | 122.63 | 1.19 | 0.662 | |
| | Z4 | 221.78 | 2.31 | 0.668 | 96.67 | 0.94 | 0.527 | |
| | | | | | | | | |
| | Z1 | 165.92 | 1.77 | 0.500 | 97.32 | 0.94 | 0.394 | |
| 20 | Z2 | 199.01 | 2.09 | 0.600 | 105.62 | 1.023 | 0.473 | |
| 03 | Z3 | 222.89 | 2.32 | 0.672 | 101.43 | 0.98 | 0.552 | |
| | Z4 | 232.61 | 2.42 | 0.701 | 124.21 | 1.203 | 0.670 | |
| | | | | | | | | |
| D4 | Z1 | 82.96 | 0.97 | 0.250 | 48.40 | 0.47 | 0.197 | |
| | Z2 | 96.00 | 1.10 | 0.289 | 50.42 | 0.49 | 0.228 | |
| U4 | Z3 | 114.65 | 1.28 | 0.346 | 53.08 | 0.51 | 0.294 | |
| | Z4 | 179.51 | 1.90 | 0.541 | 87.48 | 0.85 | 0.478 | |

Table 6. Vault (X) comparison of improved nonlinear static procedures (FEMA 440).

 Table 7. Vault (Y) comparison of improved nonlinear static procedures (FEMA 440).

| Seismic | Site | Equiv | Equivalent linearization | | | Displacement modification | | | |
|------------|-------|--------|--------------------------|------|----------------------|---------------------------|-------|--|--|
| zone | Class | V(kN) | D(mm) | Sa | V _{y(} (kN) | D _y (mm) | Sa | | |
| | Z1 | 334.04 | 15.54 | 1.00 | 241.78 | 10.52 | 0.825 | | |
| | Z2 | 334.04 | 15.54 | 1.00 | 230.52 | 10.03 | 0.825 | | |
| D1 | Z3 | 367.44 | 16.93 | 1.10 | 238.60 | 10.38 | 0.907 | | |
| | Z4 | 300.64 | 14.15 | 0.90 | 190.15 | 8.27 | 0.742 | | |
| | Z1 | 250.53 | 12.06 | 0.75 | 179.08 | 7.80 | 0.619 | | |
| 50 | Z2 | 275.59 | 13.11 | 0.83 | 187.54 | 8.16 | 0.681 | | |
| D2 | Z3 | 300.64 | 14.15 | 0.90 | 190.15 | 8.28 | 0.742 | | |
| | Z4 | 300.64 | 14.15 | 0.90 | 190.15 | 8.28 | 0.742 | | |
| | Z1 | 167.02 | 8.58 | 0.50 | 99.72 | 4.34 | 0.352 | | |
| D 2 | Z2 | 200.43 | 9.97 | 0.60 | 133.96 | 5.83 | 0.495 | | |
| D3 | Z3 | 233.83 | 11.37 | 0.70 | 143.98 | 6.27 | 0.578 | | |
| | Z4 | 283.94 | 13.45 | 0.85 | 178.39 | 7.76 | 0.701 | | |
| D4 | Z1 | 83.51 | 5.10 | 0.25 | 57.94 | 2.52 | 0.207 | | |
| | Z2 | 100.21 | 5.80 | 0.30 | 65.39 | 2.85 | 0.247 | | |
| | Z3 | 125.27 | 6.84 | 0.38 | 78.95 | 3.44 | 0.330 | | |
| | Z4 | 192.07 | 9.63 | 0.58 | 127.25 | 5.54 | 0.516 | | |

is one of the important parameters. 3. For Flat vault models, each result is significantly different.

4. Support conditions on top of the columns for spatial

structures were found very effective in earthquake behavior of the systems. Further research is necessary for this part.

As a result of the study, structural geometry, earthquake zone and soil class affect the analysis results in each method. Results with Displacement Modification and Equivalent Linearization defined in FEMA are different for each type of structural systems. Therefore, when designing these types of structures, designers should be aware of the structural details such as geometry, structural type and support conditions.

REFERENCES

- Applied Technology Council (1996). Seismic evaluation and retrofit of concrete buildings ATC-40. California;
- Applied Technology Council (2005). Improvements of nonlinear static seismic analysis procedures. Redwood City (CA): FEMA- p440;
- Ay Z (1994). Free Vibration and Dynamic Response of Spatial Steel Space Structures Subjected to Impulsive Excitations, PhD Thesis, Technical University of Istanbul. TR.
- Ay Z, Durmuş G (2002). "Issues of Prefabricated Steel Structures in Engineering Practice" Engineering News. 47/2002-2: 418.
- Aydinoglu MN (2003). An incremental response spectrum analysis procedure based on inelastic spectral displacements for multi-mode seismic performance evaluation. Bull. Earth. Eng., 1(1): 3-36.
- Bozorgina Y, Bertero VV (2004). Earthquake Engineering From Engineering Seismology to Performance- Based Engineering, Crc Press.
- Chintanapakdee C, Chopra AK (2003). Evaluation of modal pushover analysis using generic frames. Earthquake Eng. Structural Dynamics, 32: 417-442.
- Chopra AK, Goel RK (1999). Capacity Demand Diagram Methods for Estimating Seismic Deformation of Inelastic Structures: SDOF Systems, report no. PEER- 1999/02
- Chopra AK, Goel RK (2002). A modal pushover procedure for estimating seismic demands for buildings. Earthquake Engineering and Structural Dynamics, 31: 561-82.
- Chopra AK, Goel RK (2004). A modal pushover procedure to estimate seismic demands for unsymmetric-plan buildings. Earthquake Eng. Structural Dynamics, 33: 903-927.

- Chopra AK, Goel RK (2004). Chintanapakdee C. Evaluation of a modified MPA procedure assuming higher modes as elastic to estimate seismic demands. Earthquake Spectra, 120(3): 757-778.
- CSI Computer, Structures Inc SAP (2000). Linear and nonlinear static and dynamic analysis of three-dimensional structures. Berkeley (CA): Computer and Structures, Inc.; 2004.
- Dikmen B, Ay Z (2006). Earthquake Response of Hall Structures with Steel Space Roof Systems", International Symposium on Advances in Civil Engineering, Ace06-486, Istanbul. TR.
- Fajfar P, EERI M (2000). A Nonlinear Analysis Method for Performance Based Design., Earthquake Spectra, 16(3): 573-592.
- Federal Emergency Management Agency (2000). Prestandard and commentary for the seismic evaluation of buildings. Washington (DC): FEMA- p.356.
- Fenkli M, Ay Z (2004). Earthquake response of Single Layer Steel Domes: Schwedler and Zeiss-Dywidag Domes", International Symposium on Advances in Civil Engineering, ACE04, Istanbul, Turkey.
- Goel RK, Chopra AK (2004). Evaluation of modal and FEMA pushover analysis: SAC buildings. Earthquake Spectra, 20(1): 225-254.
- Gupta B, Kunnath SK (2000) Adaptive spectra-based pushover procedure for seismic evaluation of structures. Earthquake Spectra, 16(2): 367-391.
- Kalkan E, Kunnath SK (2007). Assessment of current nonlinear static procedures for seismic evaluation of buildings. Eng. Struct., 29(3): 305-316.
- Korkmaz KA, Ay Z, Çelik ID (2008). Investigation of Inelastic Behavior of Concentric and Eccentric Braced Steel Building Type Structures, European Conference on Steel and Composite Structures, Graz, Avusturya, Eylül.
- Kunnath SK, Kalkan E (2004). Evaluation of seismic deformation demands using nonlinear procedures in multistory steel and concrete moment frames. ISET, J. Earth. Technol., 41(1): 159-182.
- Makowski ZS (1988), History of the Development of Braced Domes, Proceedings of IA.S-S.-M.S.U. Symposium, Istanbul. TR.
- Naeim F (2003). The Seismic Design Handbook (Second Edition), Kluwer Academic Publisher USA. Chilton J. (2000), Space Grid Structures, Architectural Pres, UK.
- Turkish Earthquake Code (2007). Ministry of Public Works and Settlement Government of Republic of Turkey, Ankara, Turkey.
- UBC (1997), Structural Engineering Design Provisions, Uniform Building Code. International Conference of Building Officials, California.